n-person Session 7

February 27, 2025

PMAP 8521: Program evaluation Andrew Young School of Policy Studies

Plan for today

do-calculus and adjustment

p-values and confidence intervals



Matching and IPW

do-calculus and adjustment

The average population-level change in y when directly intervening (or doing) x

The average population-level change in y when accounting for observed x

 $E(y \mid do(x)) \neq E(y \mid x)$ Causation
Correlation

DAGs and identification

DAGs are a statistical tool, but they don't tell you what statistical method to use

DAGs help you with the **identification strategy**



Thomas Massie @RepThomasMassie

Over 70% of Americans who died with COVID, died on Medicare, and some people want #MedicareForAll?

11:00 AM · Feb 9, 2022 · Twitter for iPhone

...

Easiest identification

Identification through research design

RCTs

When treatment is randomized, delete all arrows going into it

No need for any do-calculus!

Most other identification

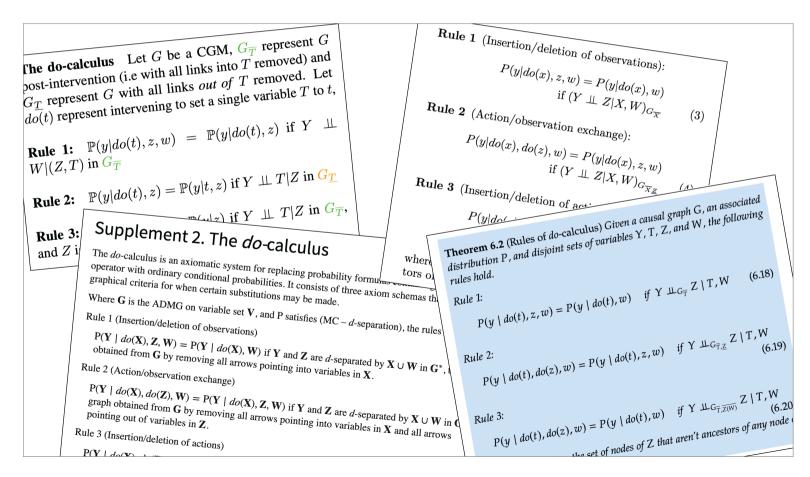
Identification through do-calculus

Rules for graph surgery

Backdoor adjustment and frontdoor adjustment are special common patterns of do-calculus

Where can we learn more about *do*-calculus?

Here!



Rule 1: Decide if we can ignore an observation

$$P(y \mid z, \operatorname{do}(x), w) = P(y \mid \operatorname{do}(x), w) \qquad ext{ if } (Y \perp Z \mid W, X)_{G_{\overline{X}}}$$

Rule 2: Decide if we can treat an intervention as an observation

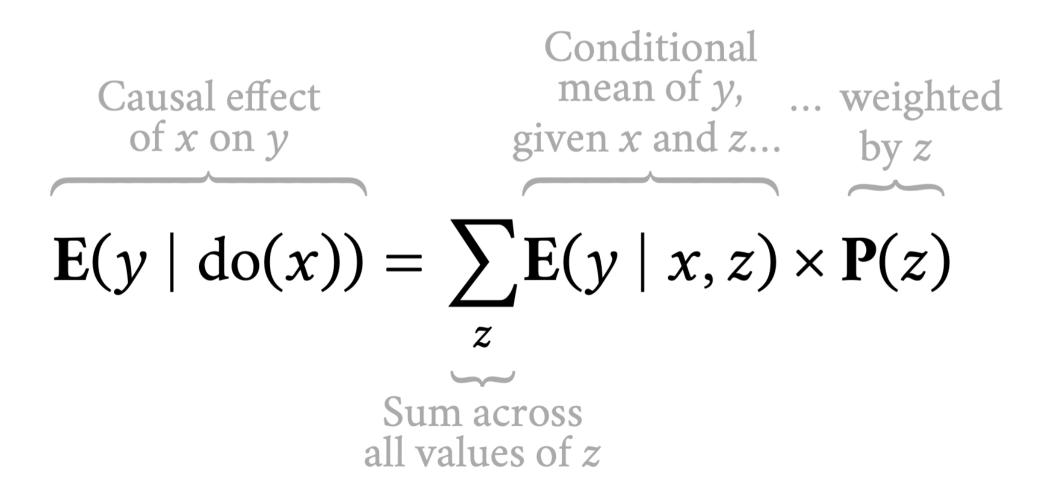
$$P(y \mid \operatorname{do}(z), \operatorname{do}(x), w) = P(y \mid z, \operatorname{do}(x), w) \qquad ext{ if } (Y \perp Z \mid W, X)_{G_{\overline{X}, Z}}$$

Rule 3: Decide if we can ignore an intervention

$$P(y \mid \operatorname{do}(z), \operatorname{do}(x), w) = P(y \mid \operatorname{do}(x), w) \qquad ext{ if } (Y \perp Z \mid W, X)_{G_{\overline{X}, \overline{Z(W)}}}$$

$$\begin{bmatrix} \text{Marginalization across } z + \text{chain rule for conditional probabilities} \end{bmatrix} \\ P(y \mid \text{do}(x)) &= \sum_{z} P(y \mid \text{do}(x), z) \times P(z \mid \text{do}(x)) \\ & [\text{Use Rule 2 to treat } \text{do}(x) \text{ as } x] \\ &= \sum_{z} P(y \mid x, z) \times P(z \mid \text{do}(x)) \\ & [\text{Use Rule 3 to nuke } \text{do}(x)] \\ &= \sum_{z} P(y \mid x, z) \times P(z \mid \text{nothing!}) \\ & [\text{Final backdoor adjustment formula!}] \\ &= \sum_{z} P(y \mid x, z) \times P(z) \end{aligned}$$

Adjusting for backdoor confounding

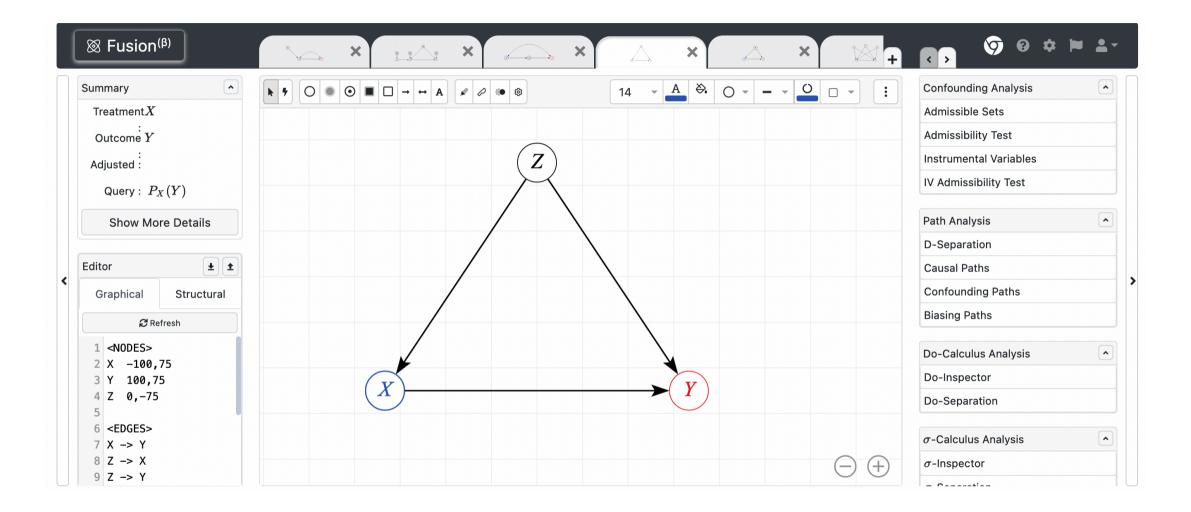


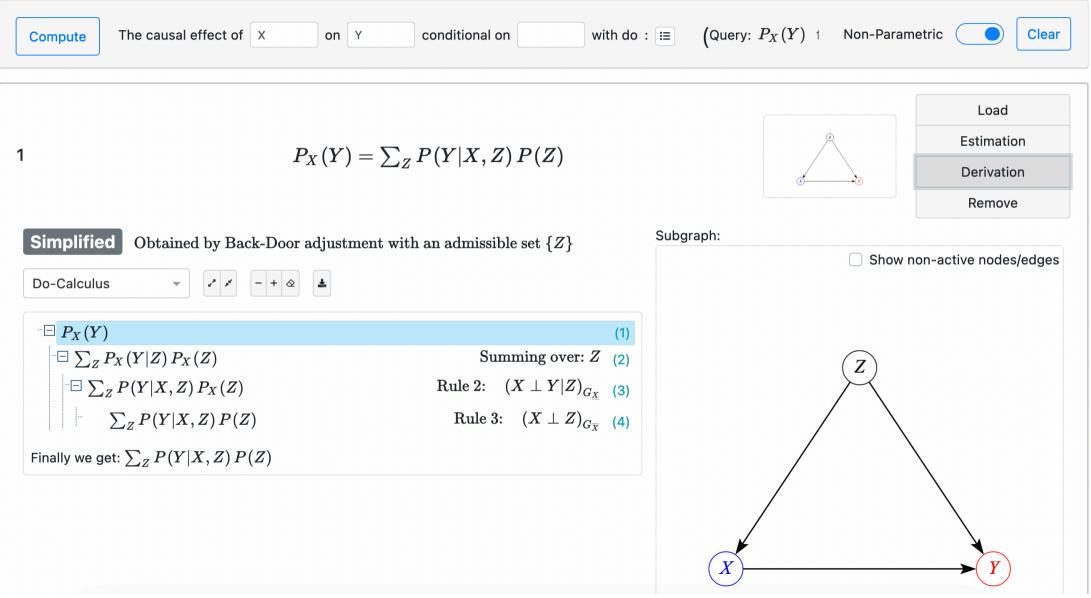
Adjusting for frontdoor confounding

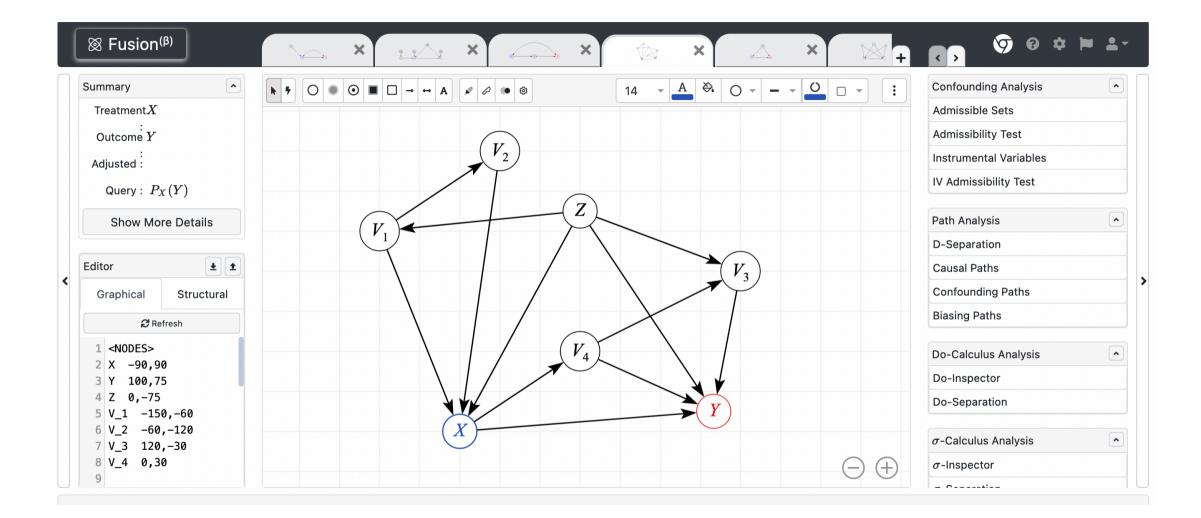
More complex DAGs without obvious backdoor or frontdoor solutions

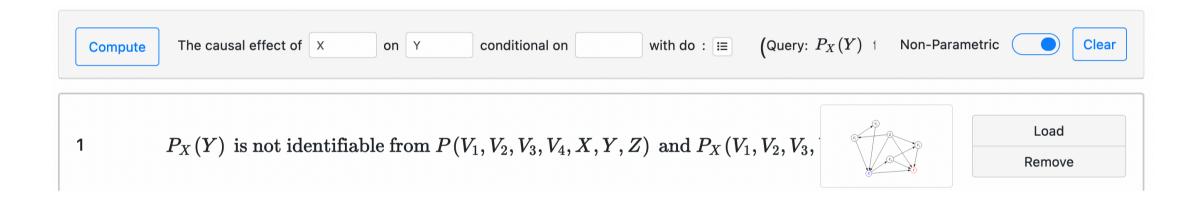
Chug through the rules of do-calculus to see if the relationship is identifiable

Causal Fusion









When things are identified, there are still arrows leading into Y. What do we do with those? How do you explain those relationships?

Outcomes have multiple causes. How do you justify that your proposed cause is the most causal factor? Does every research question need an identification strategy?

No!

Correlation alone is okay! Can lead to more focused causal questions later!

≡Forbes

BREAKING | Jan 14, 2022, 12:34pm EST | 145,393 views

Moderna Starts Human Trials Of mRNA Vaccine For Virus That Likely Causes Multiple Sclerosis

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Robert Hart Forbes Staff Business

I cover breaking news.

Listen to article 3 minutes

TOPLINE Moderna recently launched early stage clinical trials for an mRNA vaccine against the Epstein-Barr virus (EBV), a common pathogen that infects almost everyone at some point in their lives, is the primary cause of mononucleosis and, according to a study published in the journal *Science* Thursday, likely causes multiple sclerosis (MS), offering hope the devastating neurological condition might be prevented.

p-values and confidence intervals

In the absence of *p*-values, I'm confused about how we report... significance?

Imbens and *p*-values

Nobody really cares about *p*-values

Decision makers want to know a number or a range of numbers some sort of effect and uncertainty

Nobody cares how likely a number would be in an imaginary null world!

Imbens's solution

Report point estimates and some sort of range

"It would be preferable if reporting standards emphasized confidence intervals or standard errors, and, even better, Bayesian posterior intervals."

Point estimate

The single number you calculate (mean, coefficient, etc.)



Greek, Latin, and extra markings

Statistics: use a sample to make inferences about a population



Letters like β_1 are the **truth**

Letters with extra markings like $\hat{\beta}_1$ are our **estimate** of the truth based on our sample



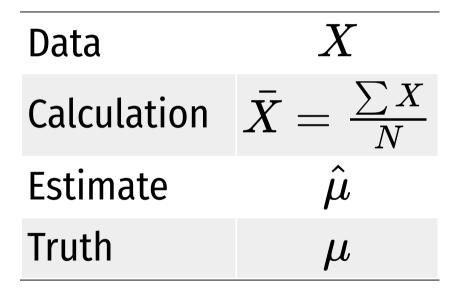
Letters like X are **actual data** from our sample

Letters with extra markings like \bar{X} are **calculations** from our sample

Estimating truth

Data \rightarrow **Calculation** \rightarrow **Estimate** \rightarrow **Truth**

X



$$ar{X} = \hat{\mu}$$

 $ightarrow ar{X}
ightarrow \hat{\mu} \xrightarrow{\mbox{ hopefully }\mbox{ hopefully }\mbox{ }\mb$

Population parameter

Truth = Greek letter

An single unknown number that is true for the entire population

Proportion of left-handed students at GSU

Median rent of apartments in Atlanta

Proportion of red M&Ms produced in a factory

Treatment effect of your program

Samples and estimates

We take a sample and make a guess

This single value is a *point estimate*

(This is the Greek letter with a hat)

Variability

You have an estimate, but how different might that estimate be if you take another sample?

Left-handedness

You take a random sample of 50 GSU students and 5 are left-handed.

If you take a different random sample of 50 GSU students, how many would you expect to be left-handed?

3 are left-handed. Is that surprising?

40 are left-handed. Is that surprising?

Nets and confidence intervals

How confident are we that the sample picked up the population parameter?

Confidence interval is a net

We can be X% confident that our net is picking up that population parameter

If we took 100 samples, at least 95 of them would have the true population parameter in their 95% confidence intervals

A city manager wants to know the true average property value of single-owner homes in her city. She takes a random sample of 200 houses and builds a 95% confidence interval. The interval is (\$180,000, \$300,000).

> We're 95% confident that the interval (\$180,000, \$300,000) captured the true mean value

WARNING

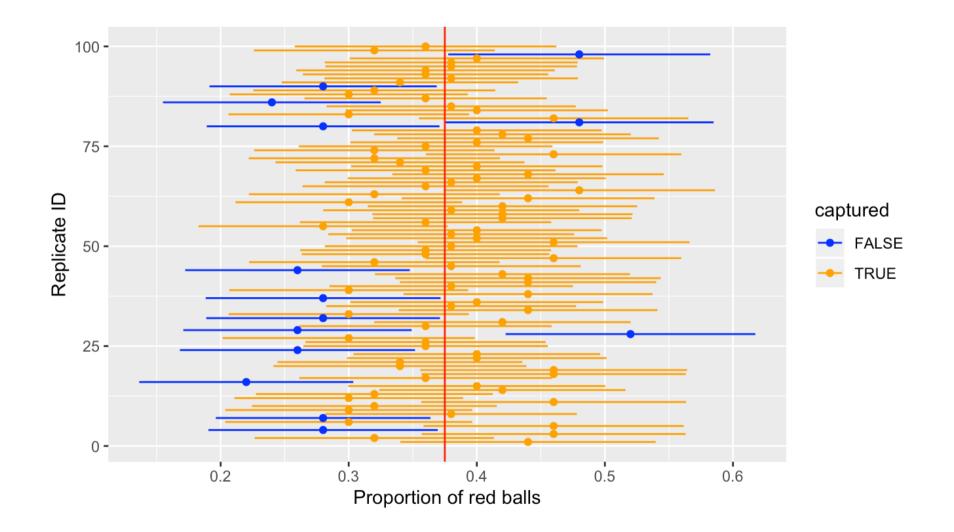
It is way too tempting to say "We're 95% sure that the population parameter is X"

People do this all the time! People with PhDs!

YOU will do this too



If you took lots of samples, 95% of their confidence intervals would have the single true value in them



Frequentism

This kind of statistics is called "frequentism"

The population parameter θ is fixed and singular while the data can vary

$P(\text{Data} \mid \theta)$

You can do an experiment over and over again; take more and more samples and polls

Frequentist confidence intervals

"We are 95% confident that this net captures the true population parameter"

> "There's a 95% chance that the true value falls in this range"

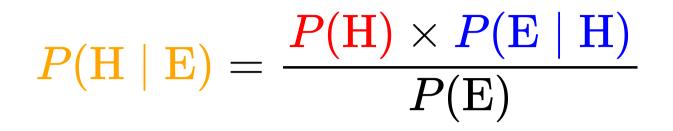
Bayesian statistics



 $P(\theta \mid \text{Data})$

$P(\mathbf{H} \mid \mathbf{E}) = rac{P(\mathbf{H}) imes P(\mathbf{E} \mid \mathbf{H})}{P(\mathbf{E})}$

Rev. Thomas Bayes



P(Hypothesis | Evidence) =

 $P(ext{Hypothesis}) imes P(ext{Evidence} \mid ext{Hypothesis})
onumber \ P(ext{Evidence})$

But the math is too hard!

So we simulate!

(Monte Carlo Markov Chains, or MCMC)

Bayesianism and parameters

In the world of frequentism, there's a fixed population parameter and the data can hypothetically vary

In the world of Bayesianism, the data is fixed (you collected it just once!) and the population parameter can vary $P(\text{Data} \mid \theta)$

 $P(\theta \mid \text{Data})$

Bayesian credible intervals

(AKA posterior intervals)

"Given the data, there is a 95% probability that the true population parameter falls in the credible interval"

Intervals

Frequentism

Bayesianism

There's a 95% probability that the range contains the true value There's a 95% probability that the true value falls in this range

Probability of the range

Few people naturally think like this

Probability of the actual value

People *do* naturally think like this!

Thinking Bayesianly

We all think Bayesianly, even if you've never heard of Bayesian stats

Every time you look at a confidence interval, you inherently think that the parameter is around that value, but that's wrong!

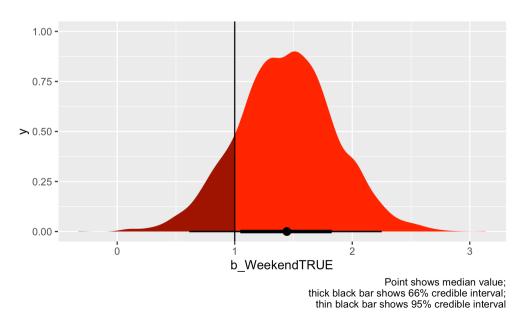
> BUT Imbens cites research that that's actually generally okay

Often credible intervals are super similar to confidence intervals

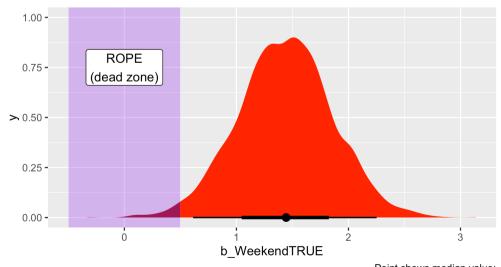
Bayesian inference

Inference without *p***-values!**

Probability of direction



Region of practical equivalence (ROPE)



Point shows median value; thick black bar shows 66% credible interval; thin black bar shows 95% credible interval 46 / 63 RCTS



Do we really not control for things in an RCT?

Randomness and arrow deletion

Balance tests



Chelsea Parlett-Pelleriti @ChelseaParlett

Trying to convince someone NOT to do t-tests to compare randomly assigned groups at baseline

no context the good place @nocontexttgp · Mar 10



1:04 PM · Mar 13, 2021 · Twitter for iPhone



Chelsea Parlett-Pelleriti @ChelseaParlett · Mar 13 THE RANDOMIZATION WORKED. RANDOMIZATION DOESN'T MEAN GROUPS WILL ALWAYS BE EQUAL

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Chelsea Parlett-Pelleriti @ChelseaParlett

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YOU DONT NEED A HYPOTHESIS TEST IF YOU KNOW THE DATA GENERATING PROCESS

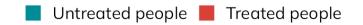
1:18 PM · Mar 13, 2021 · Twitter for iPhone

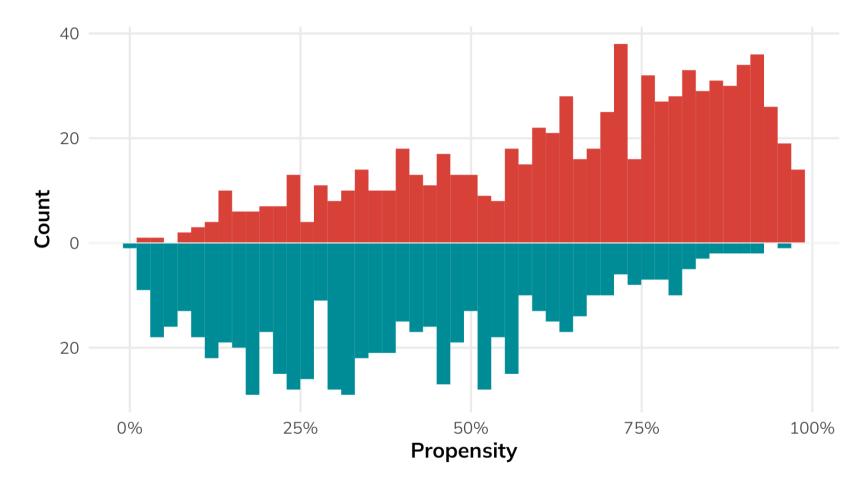
Can you walk through an example of RCTs in class?

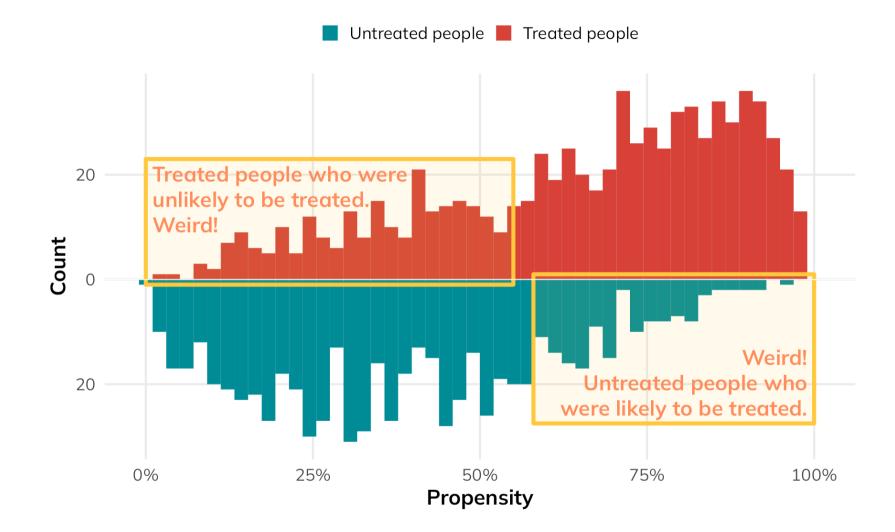
Matching and IPW

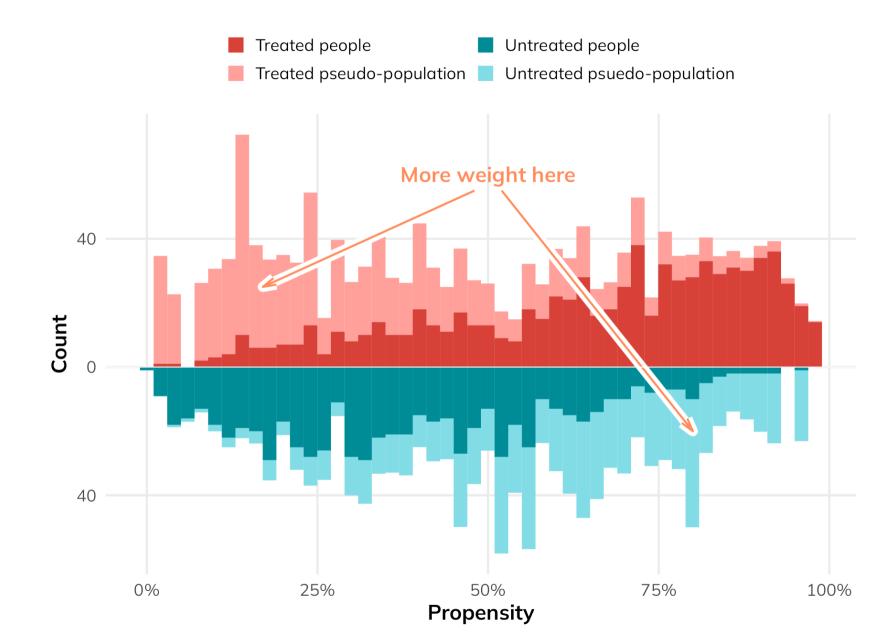
Can you talk more about propensity scores and "weirdness" weights?

Lecture slide









Why not just control for confounders instead of doing the whole matching/IPW dance?

Do you have to use logistic regression + OLS for IPW?

No!

Which should we use? Matching or IPW?

Can you walk through an example of IPW and matching in class?