

Measurement and DAGs

Session 4

PMAP 8521: Program evaluation
Andrew Young School of Policy Studies

Plan for today

**Abstraction, stretching,
and validity**

Causal models

Paths, doors, and adjustment

Abstraction, stretching, and validity

Indicators

Inputs, activities, and outputs

Generally directly measurable

of citations mailed,
% increase in grades, etc.

Outcomes

Harder to measure directly

Loftier and more abstract

Commitment to school,
reduced risk factors

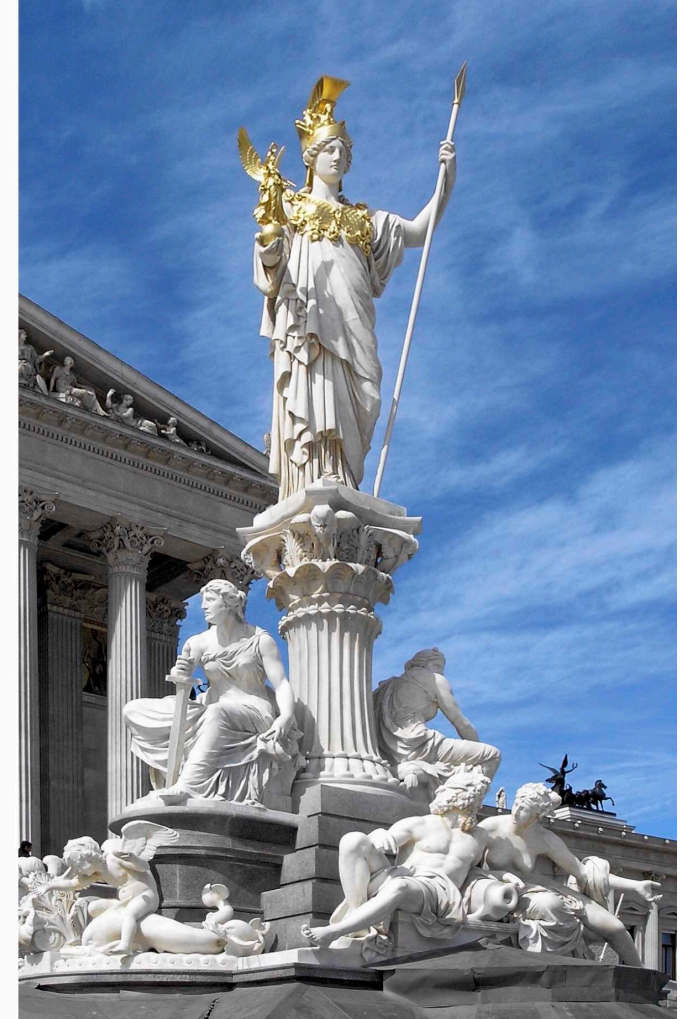
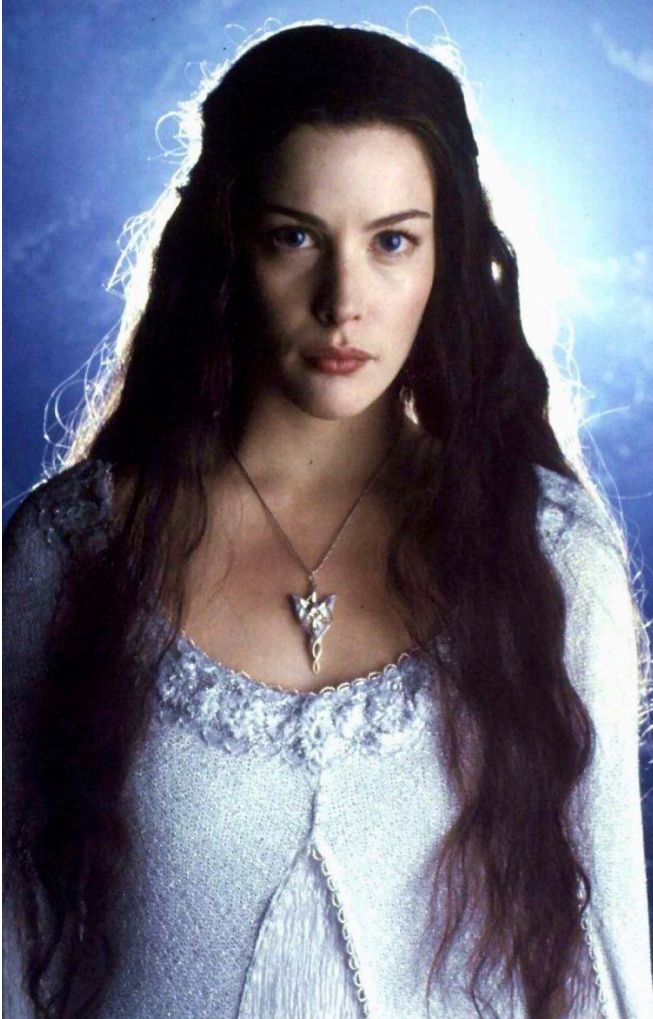
**How do you measure
abstract outcomes?**

Move up the ladder of abstraction.





Conceptual stretching



Ladder of abstraction for witches

Mammal

Enmagicked

Trolls, elves, gods/goddesses

Female

Arwen, Winky, Athena

Human

Young

Salem witch trials

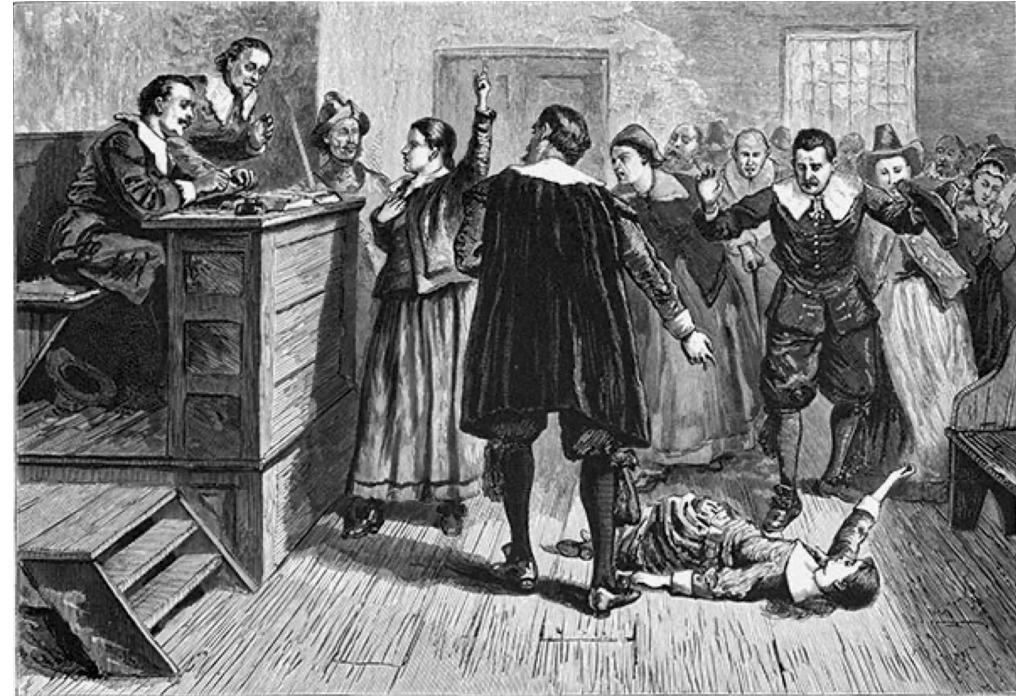
Student

Hermione Granger,
Sabrina Spellman

Old

Elphaba, Halloween decorations

Connection to theory



Outcomes and programs

Outcome variable

Thing you're measuring

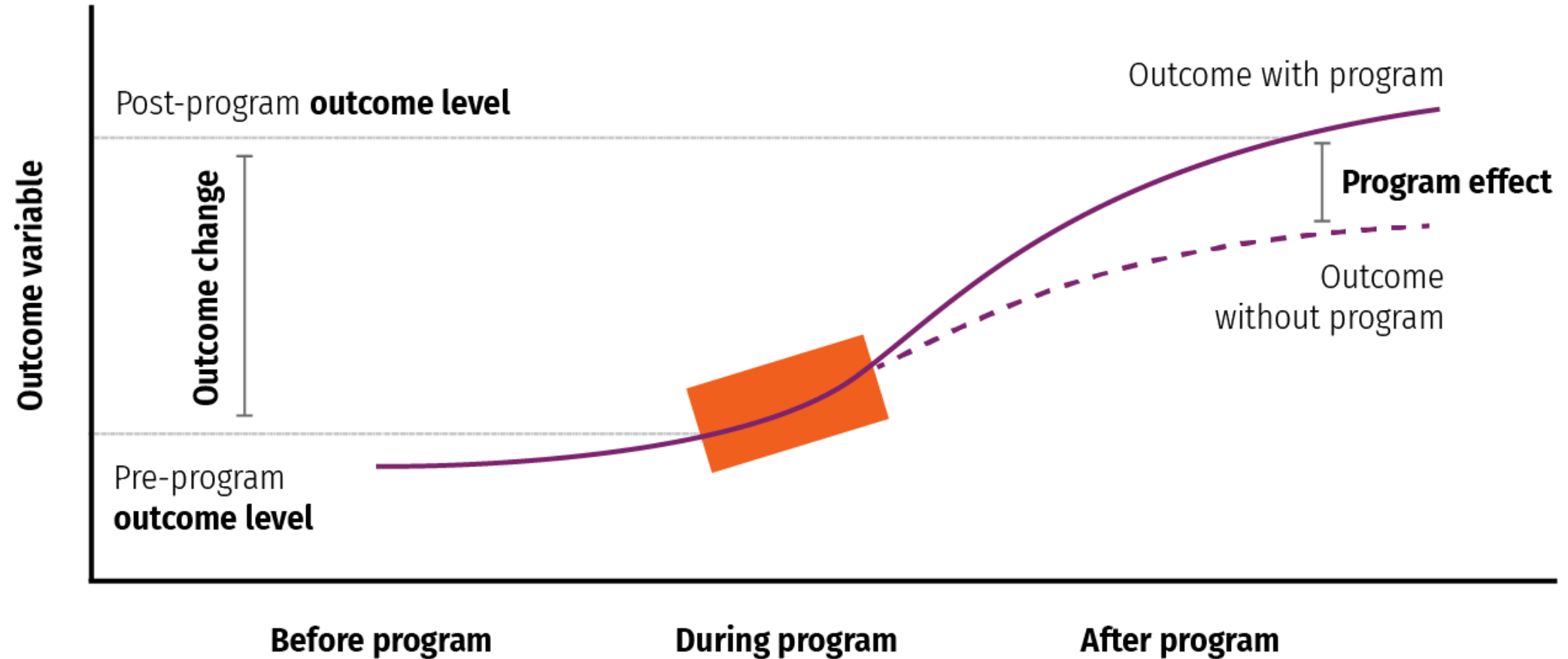
Outcome change

Δ in thing you're measuring over time

Program effect

Δ in thing you're measuring over time *because of* the program

Outcomes and programs



Connecting measurement to programs

Measurable definition of program effect

Ideal measurement

Feasible measurement

Connection to real world

Causal models

Types of data

Experimental

You have control over which units get treatment

Observational

You don't have control over which units get treatment

Which kind lets you prove causation?

Causation with observational data

**Can you prove causation
with observational data?**

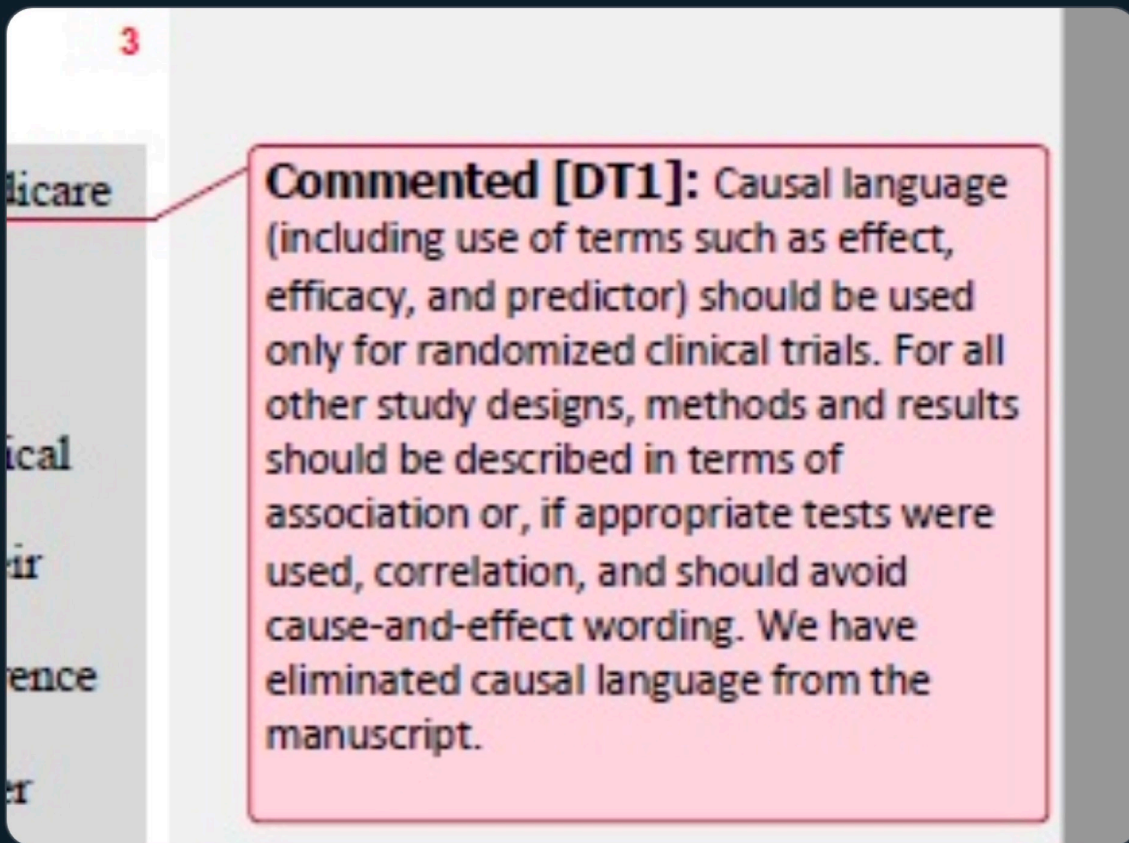
**Why is it so controversial
to use observational data?**



Laura Hatfield
@laura_tastic

Wow: this comment from fresh page proofs.

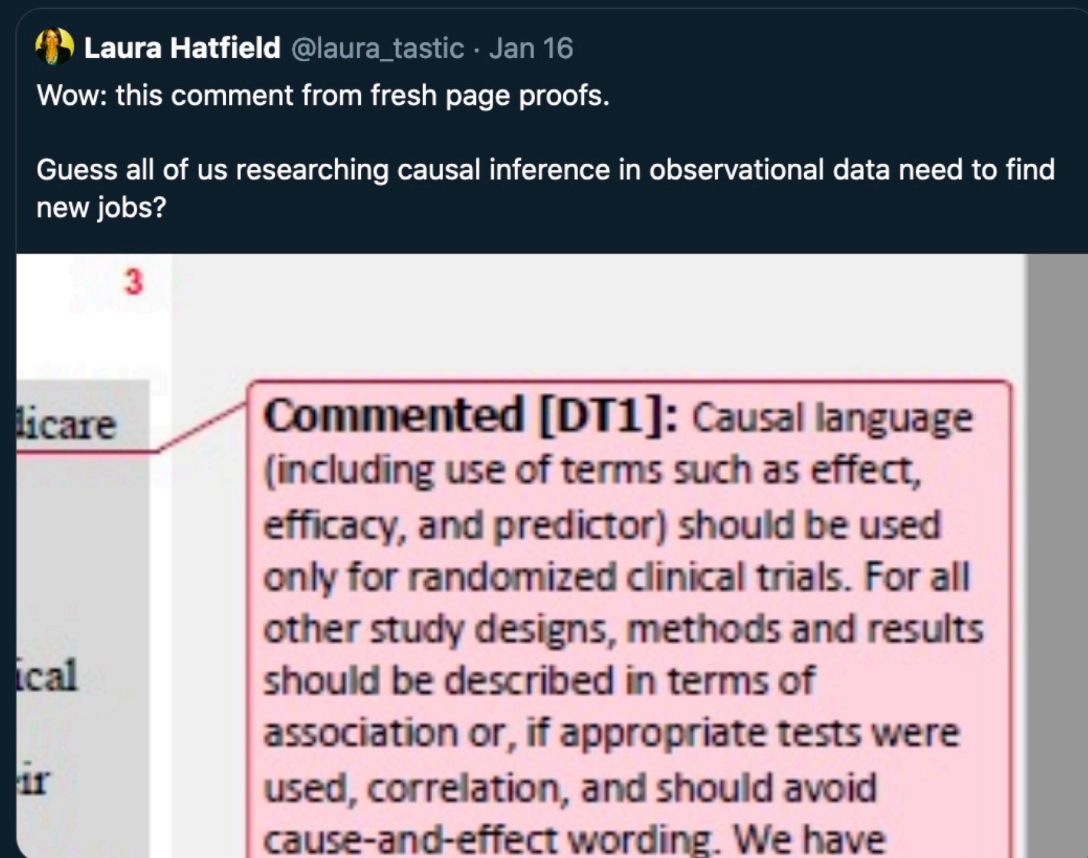
Guess all of us researching causal inference in observational data need to find new jobs?



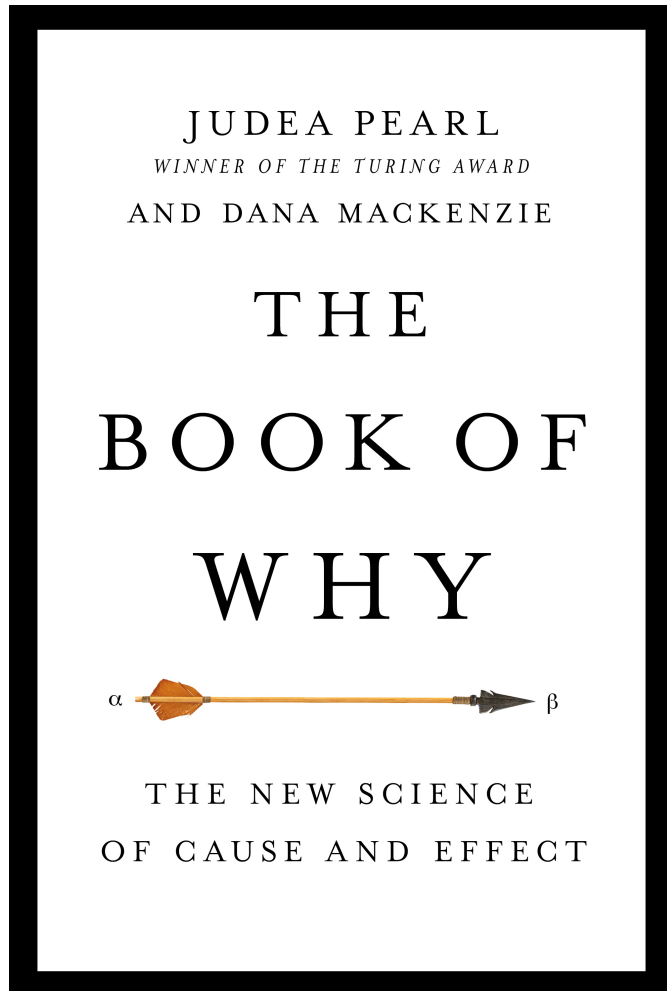
Seva
@SevaUT

normal person: this rain is making us wet

me, RCT genius: whoa there! First, take twenty walks and randomly apply the rain treatment



The causal revolution



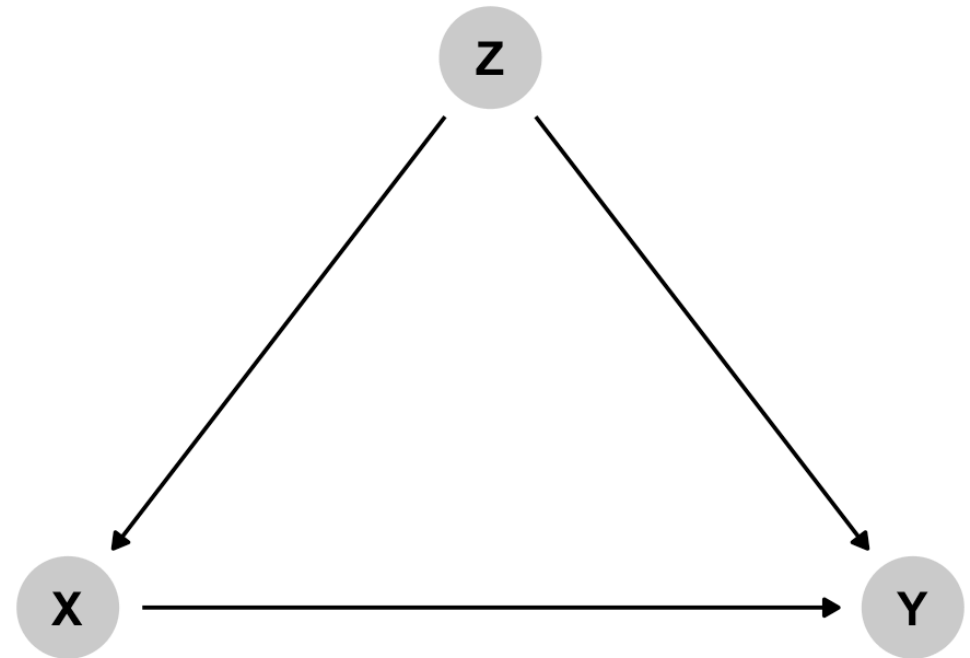
Causal diagrams

Directed acyclic graphs (DAGs)

Directed: Each node has an arrow that points to another node

Acyclic: You can't cycle back to a node (and arrows only have one direction)

Graph: It's... um... a graph



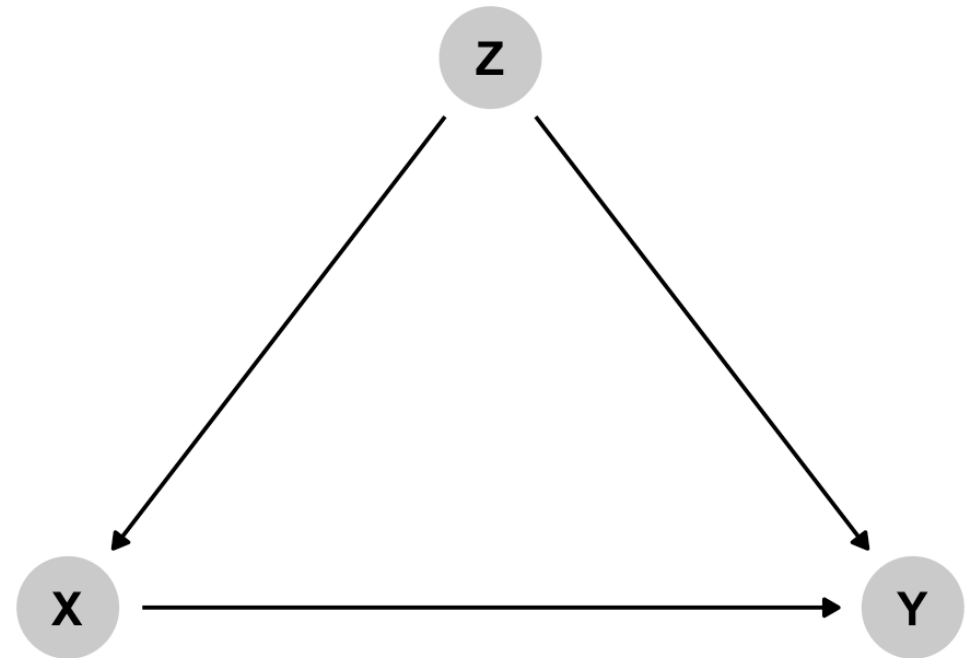
Causal diagrams

Directed acyclic graphs (DAGs)

Graphical model of the process
that generates the data

Maps your philosophical model

Fancy math ("*do*-calculus") tells
you what to control for to isolate
and identify causation



Acyclicalness

What if there's something that really is cyclical?

Wealth $\rightarrow$ Power $\rightarrow$ Wealth

This isn't acyclic!
Wealth $\leftrightarrow$ Power

Split the node into different time periods

Wealth _{$t-1$} $\rightarrow$ Power _{t} $\rightarrow$ Wealth _{t}

How to draw a DAG

What is the causal effect of an additional year of education on earnings?

Step 1: List variables

Step 2: Simplify

Step 3: Connect arrows

Step 4: Use logic and math to determine which nodes and arrows to measure

1. List variables

Education (treatment) → Earnings (outcome)

Location

Ability

Demographics

Socioeconomic status

Year of birth

Compulsory schooling laws

Job connections

2. Simplify

Education (treatment) → Earnings (outcome)

Location

Ability

Demographics

Socioeconomic status

Year of birth

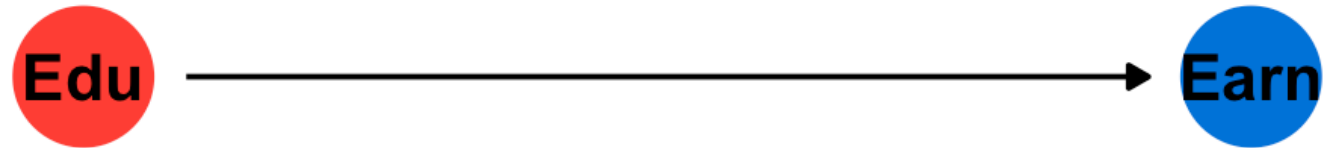
Compulsory schooling laws

Job connections

Background

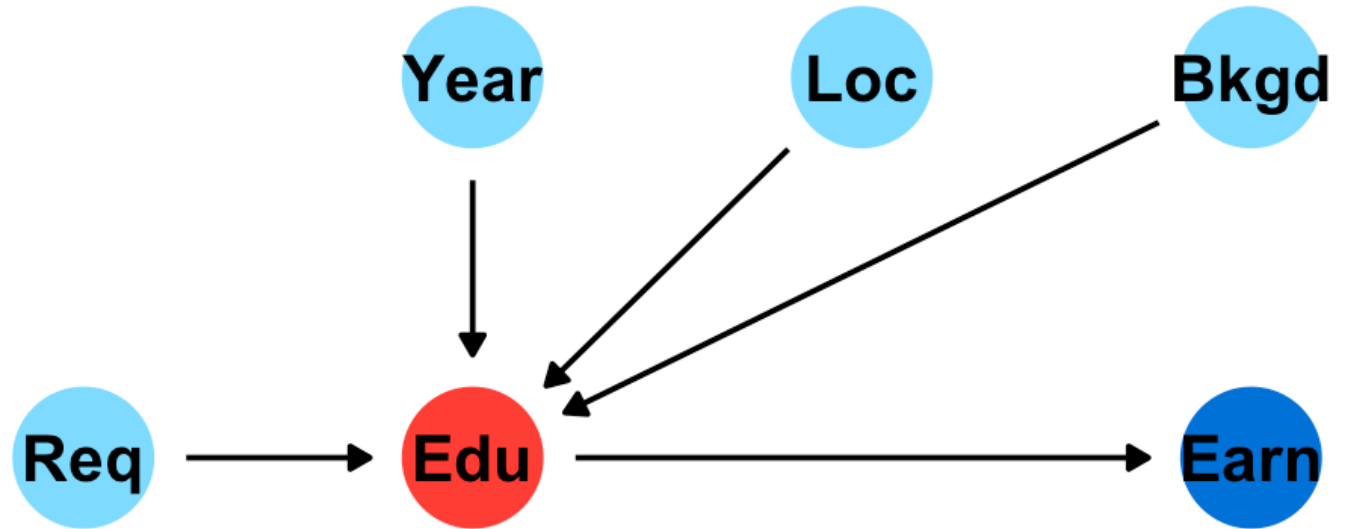
3. Draw arrows

Education causes
earnings



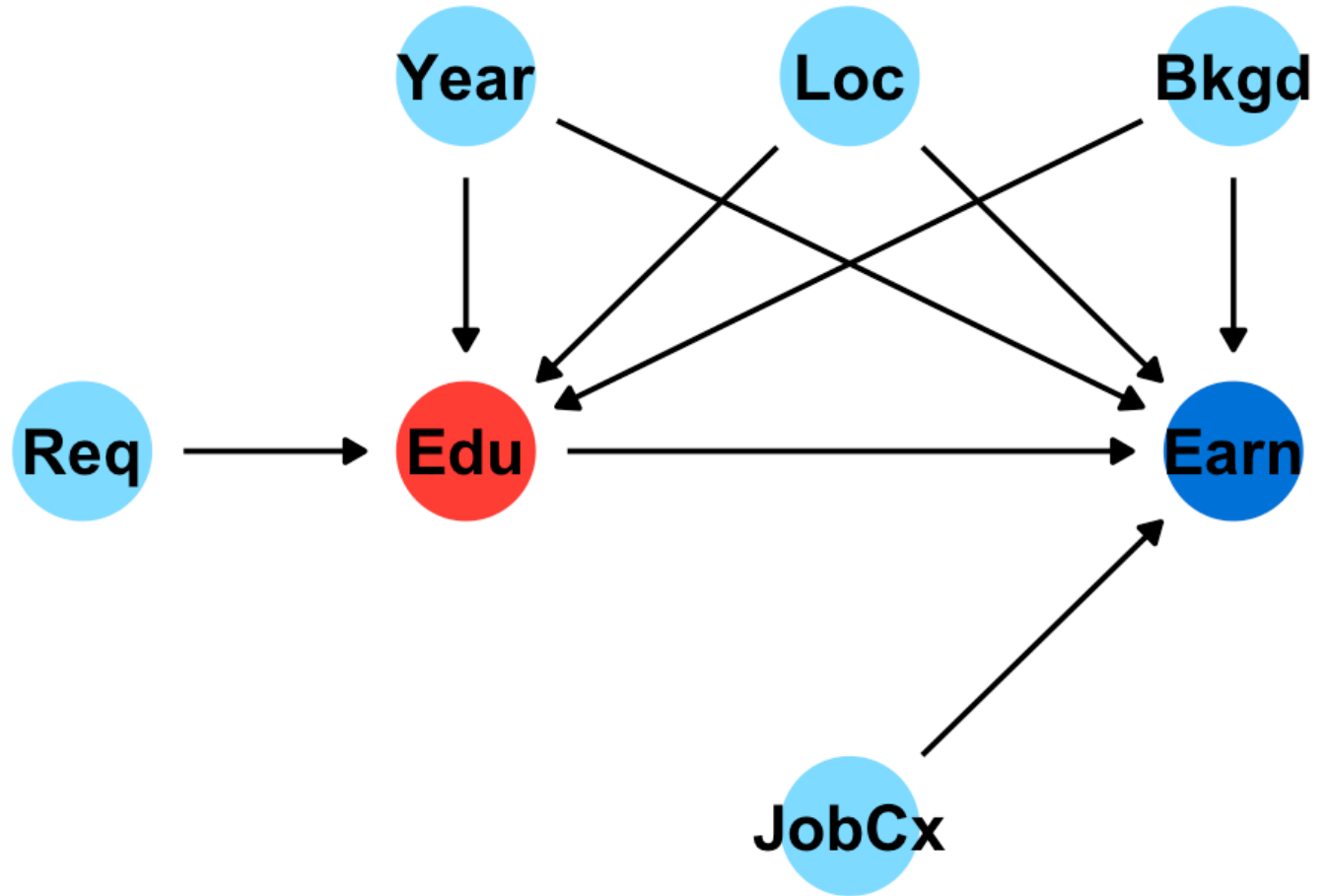
3. Draw arrows

Background, year of birth, location, job connections, and school requirements all cause education



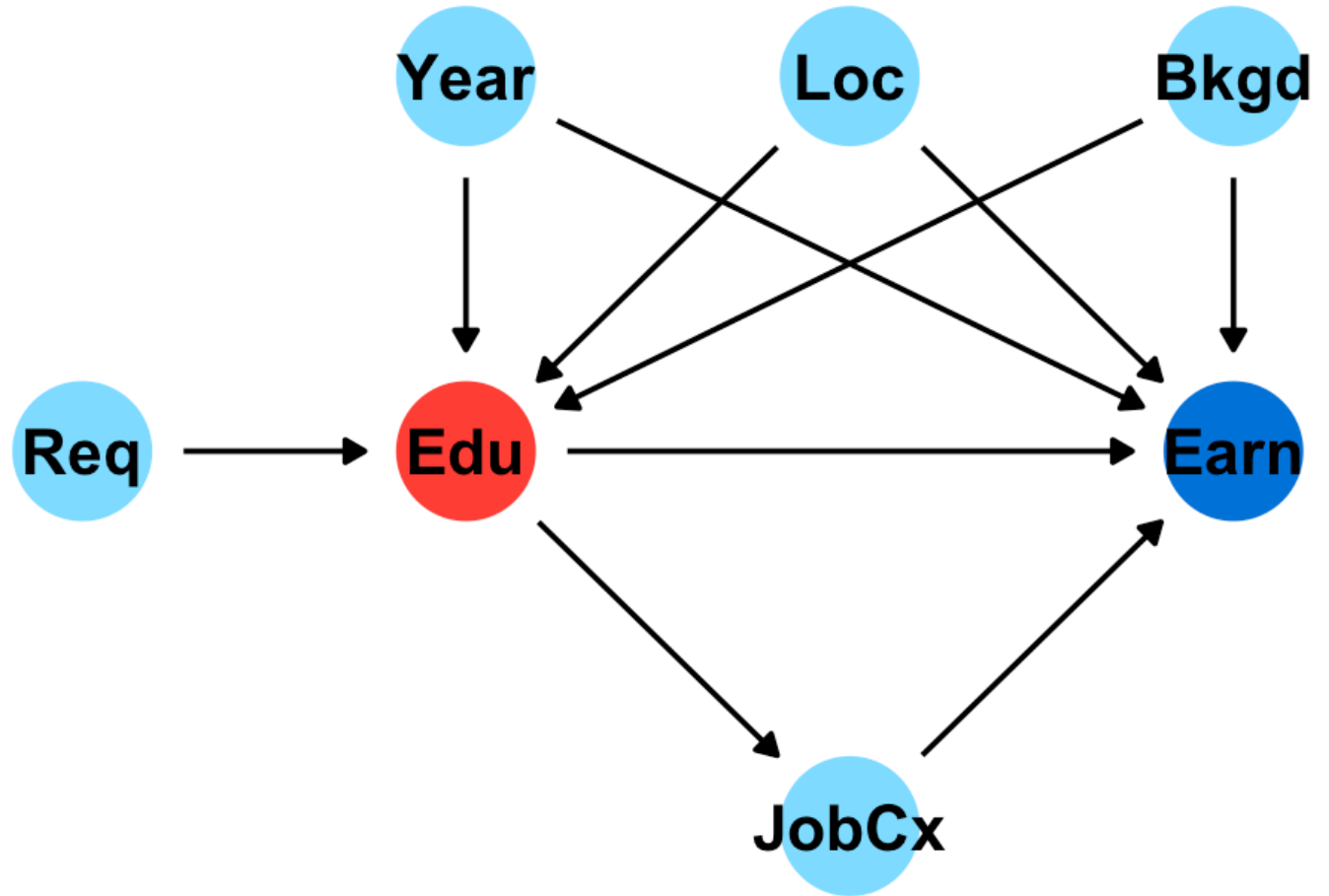
3. Draw arrows

Background, year of birth, and location all cause earnings too



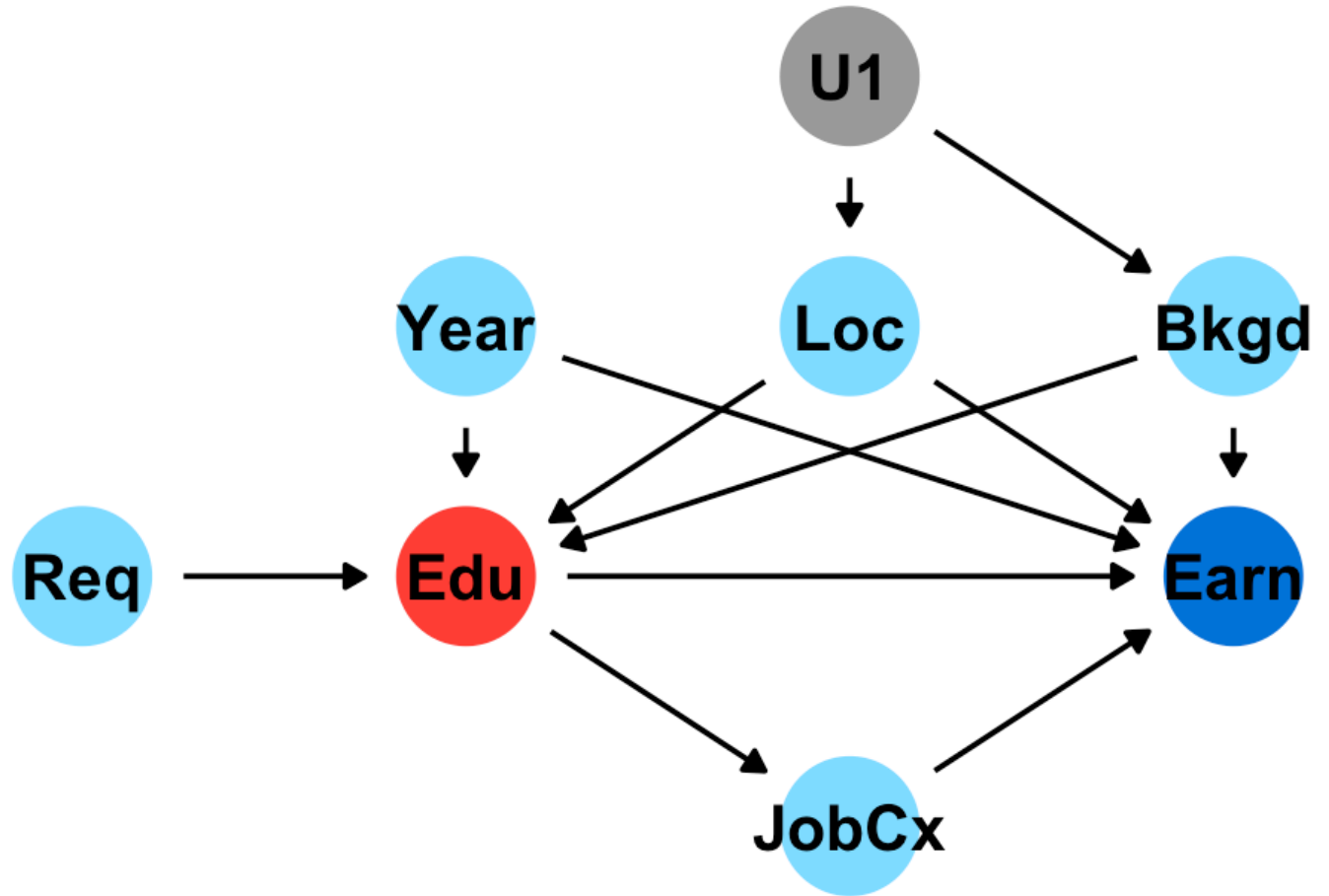
3. Draw arrows

Education causes
job earnings



3. Draw arrows

Location and background are probably related, but neither causes the other. Something unobservable (U1) does that.



Let the computer do this!

dagitty.net

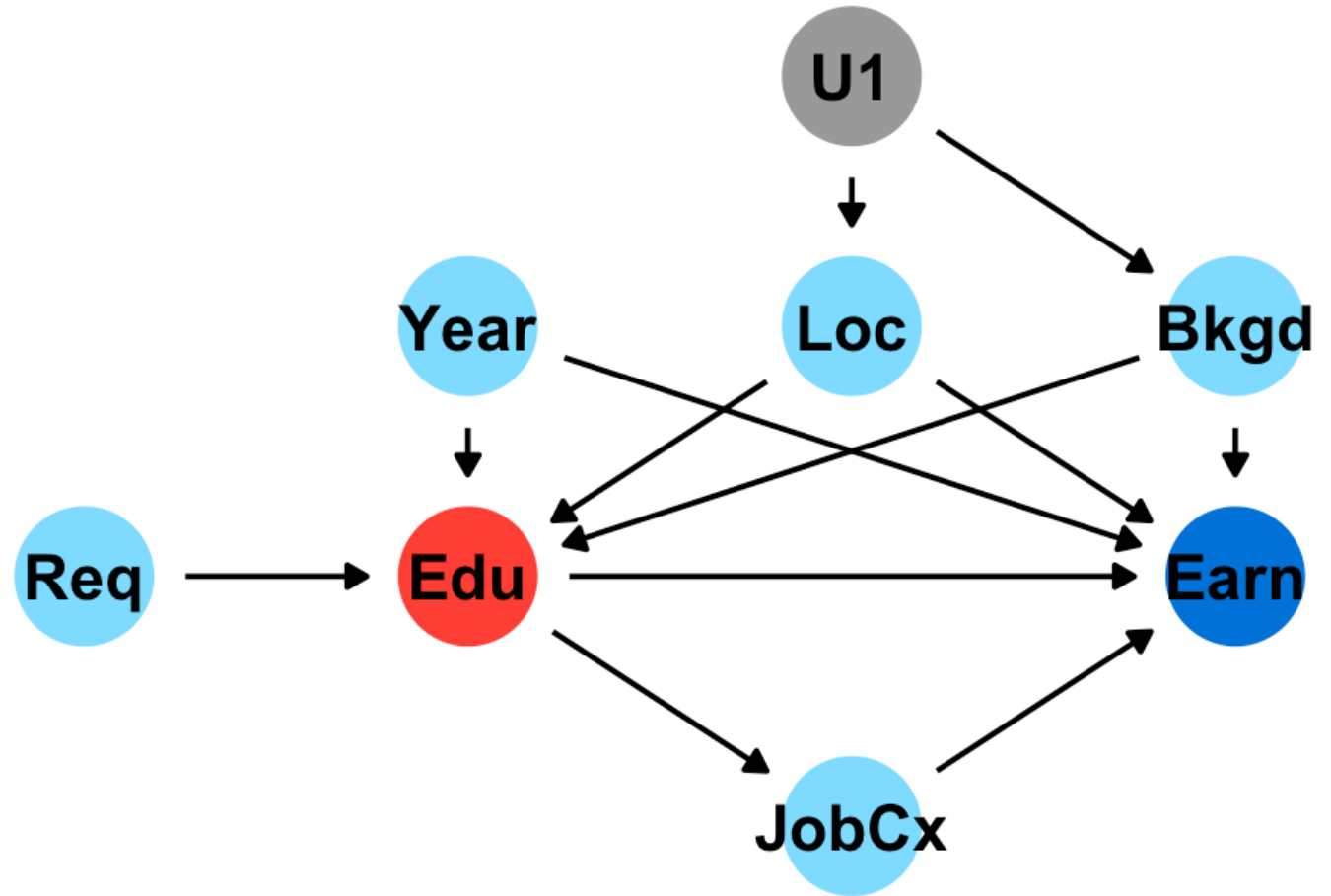
ggdag package in R

Paths, doors, and adjustment

Causal identification

All these nodes are related; there's correlation between them all

We care about $\text{Edu} \rightarrow \text{Earn}$, but what do we do about all the other nodes?



Causal identification

A causal effect is *identified* if the association between treatment and outcome is properly stripped and isolated

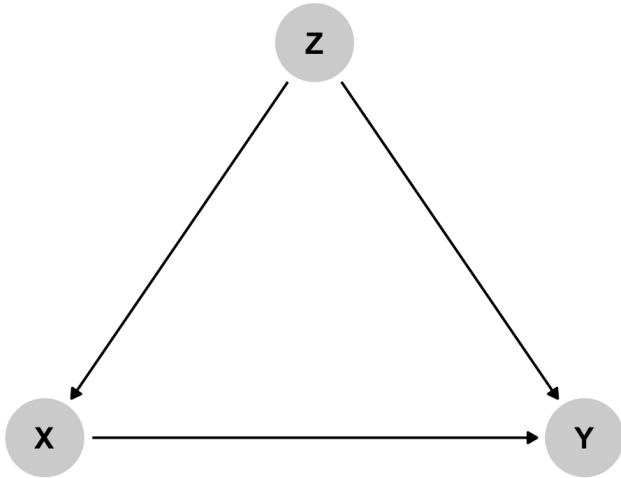
Paths and associations

Arrows in a DAG transmit associations

**You can redirect and control those paths by
"adjusting" or "conditioning"**

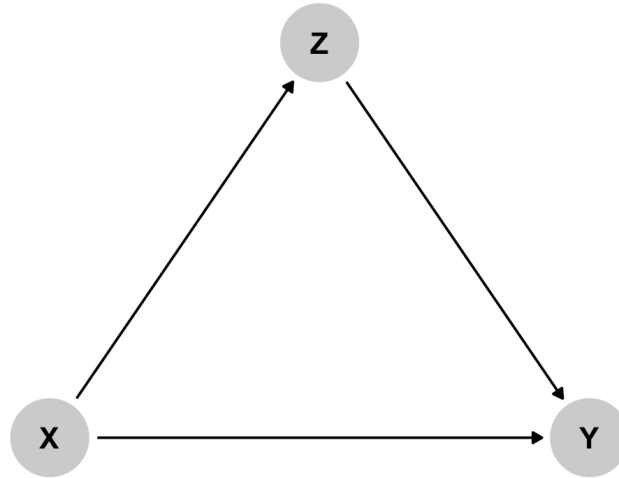
Three types of associations

Confounding



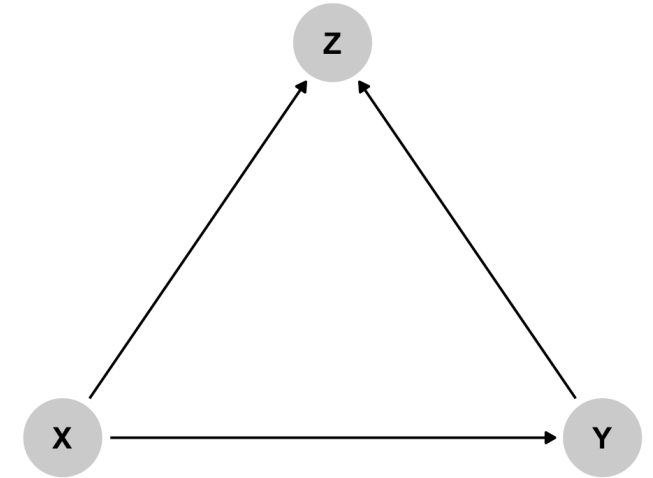
Common cause

Causation



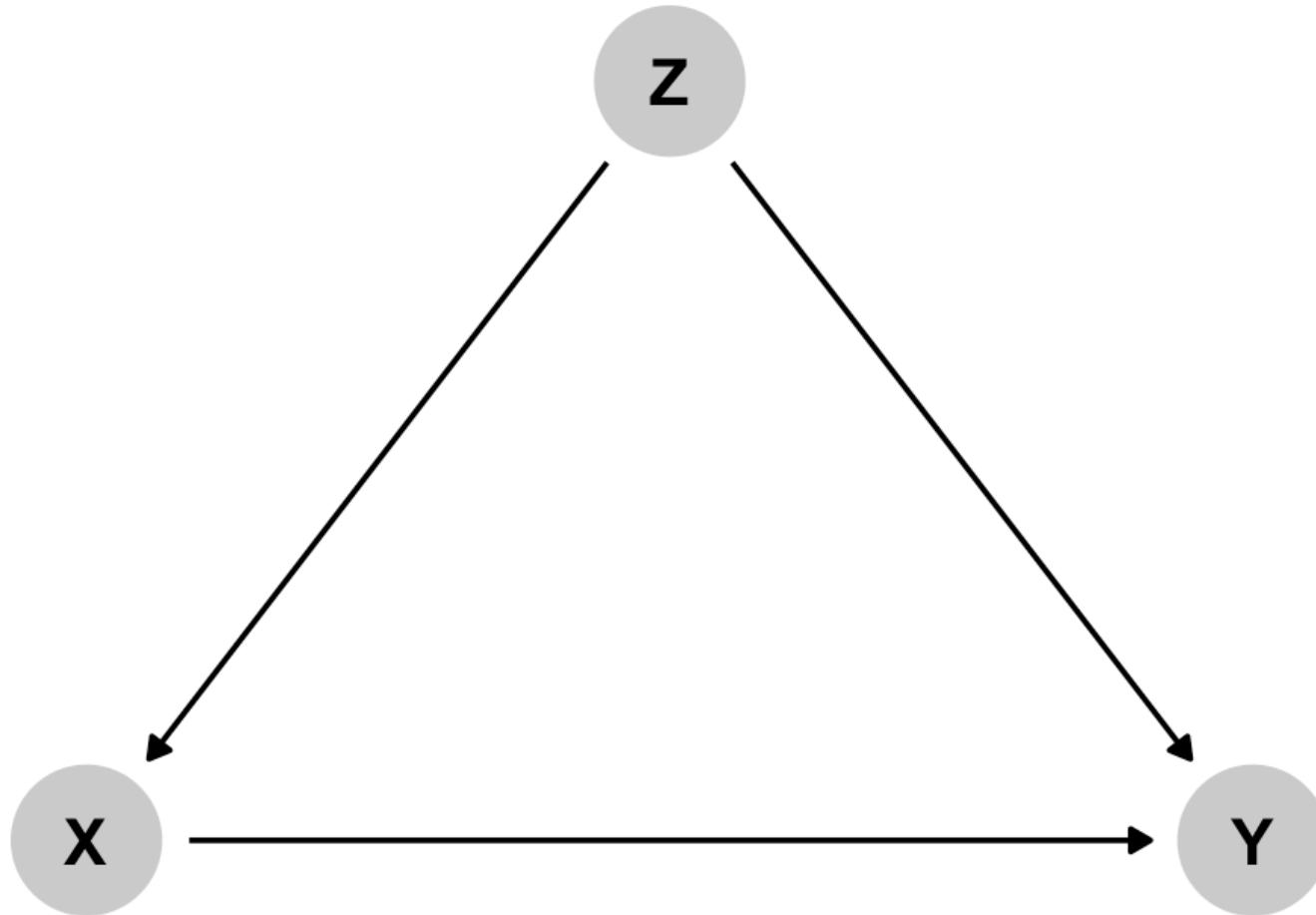
Mediation

Collision



Selection /
endogeneity

Confounding

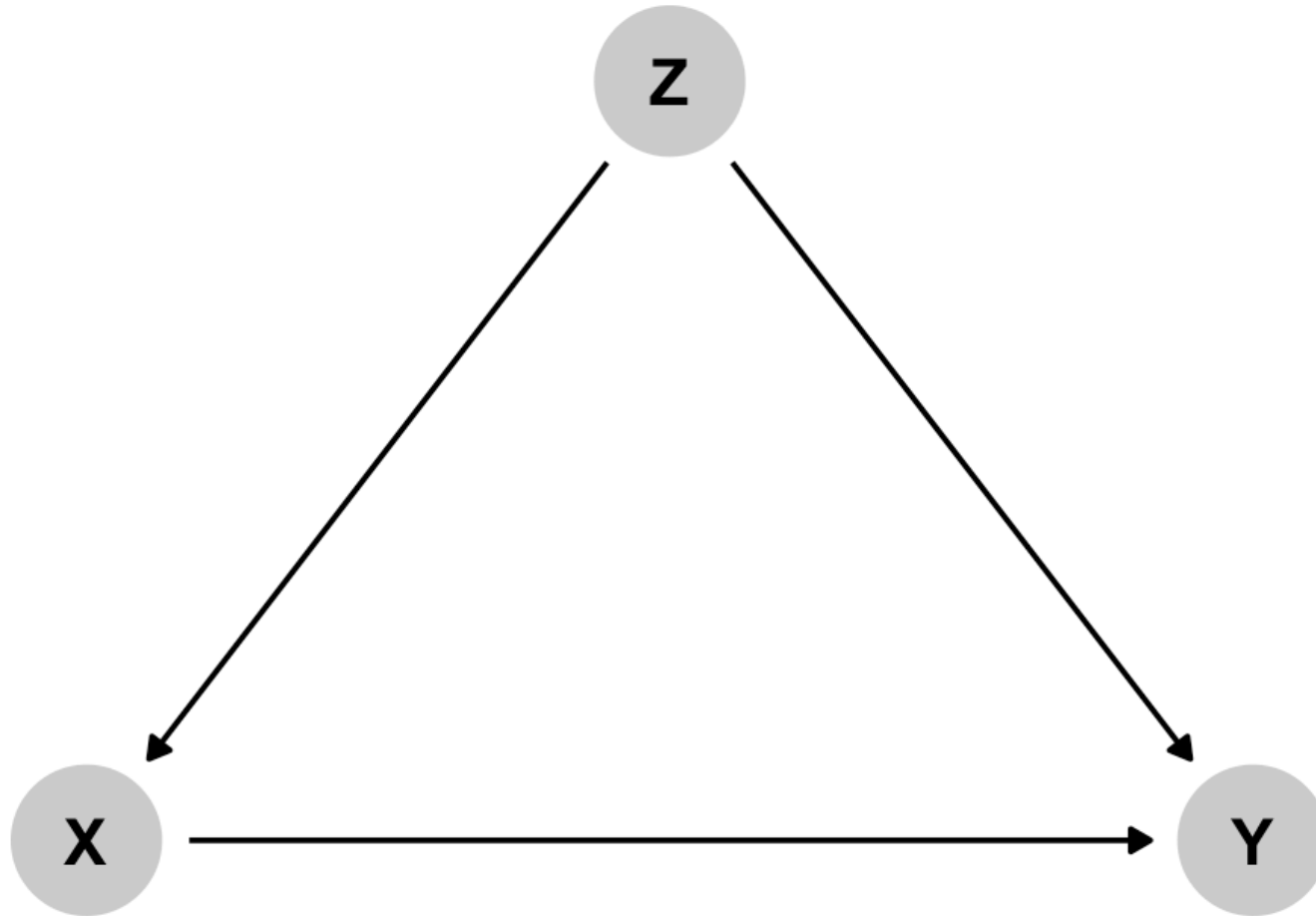


X causes Y

But Z causes both X and Y

Z confounds the $X \rightarrow Y$ association

Paths



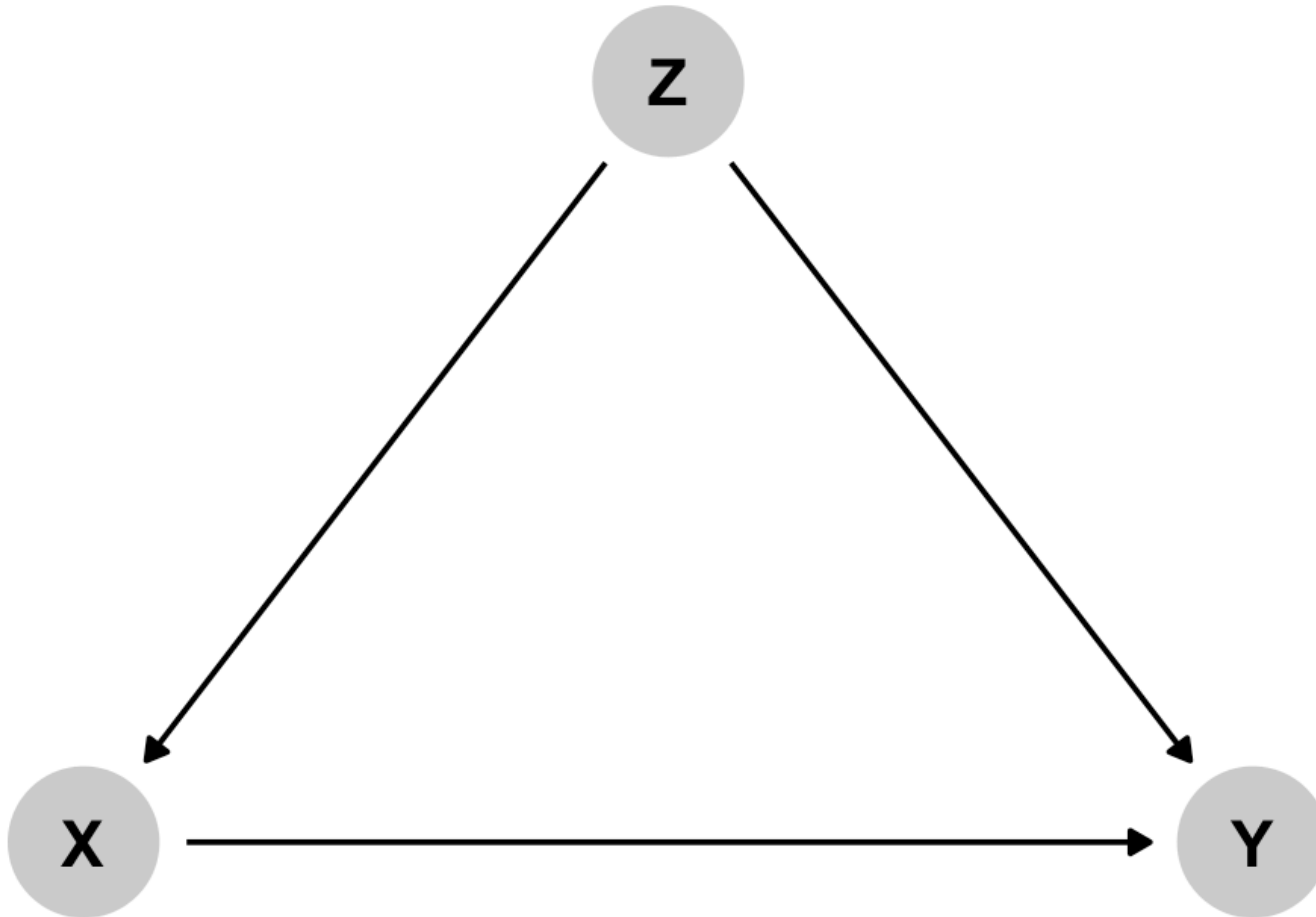
Paths between
X and Y?

$X \rightarrow Y$

$X \leftarrow Z \rightarrow Y$

**Z is a
*backdoor***

d-connection

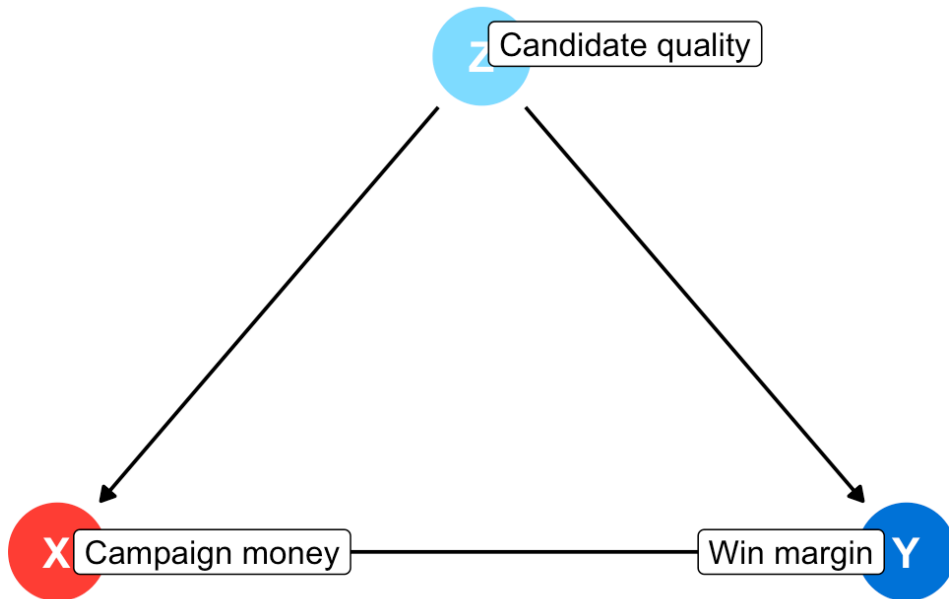


**X and Y are
"d-connected"
because
associations can
pass through Z**

**The relationship
between X and Y is
not identified /
isolated**

Effect of money on elections

What are the paths
between **money** and **win margin**?



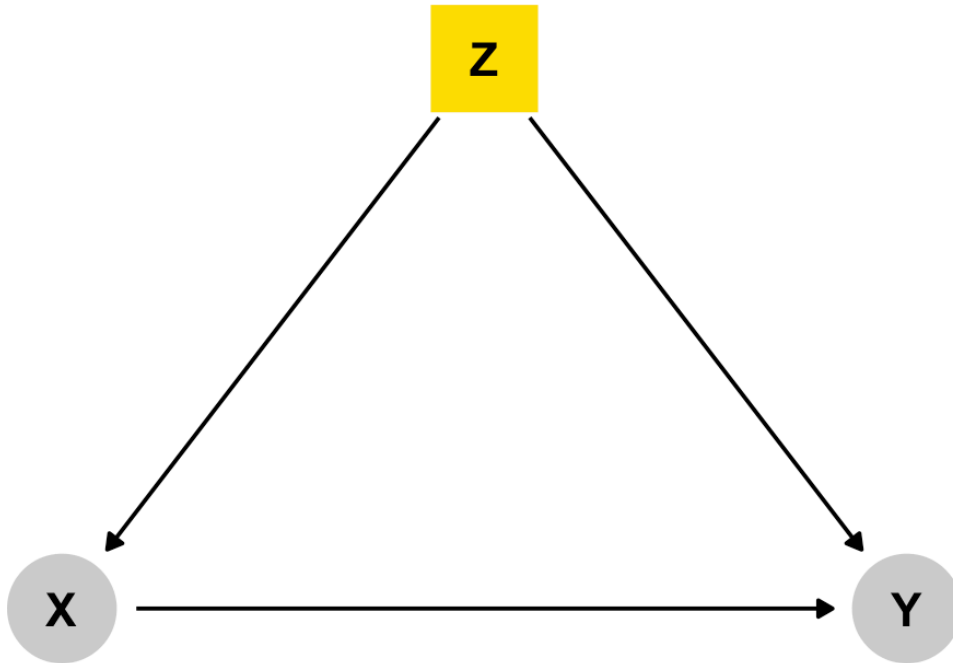
Money → Margin

Money ← Quality → Margin

Quality is a *backdoor*

Closing doors

**Close the backdoor
by adjusting for Z**

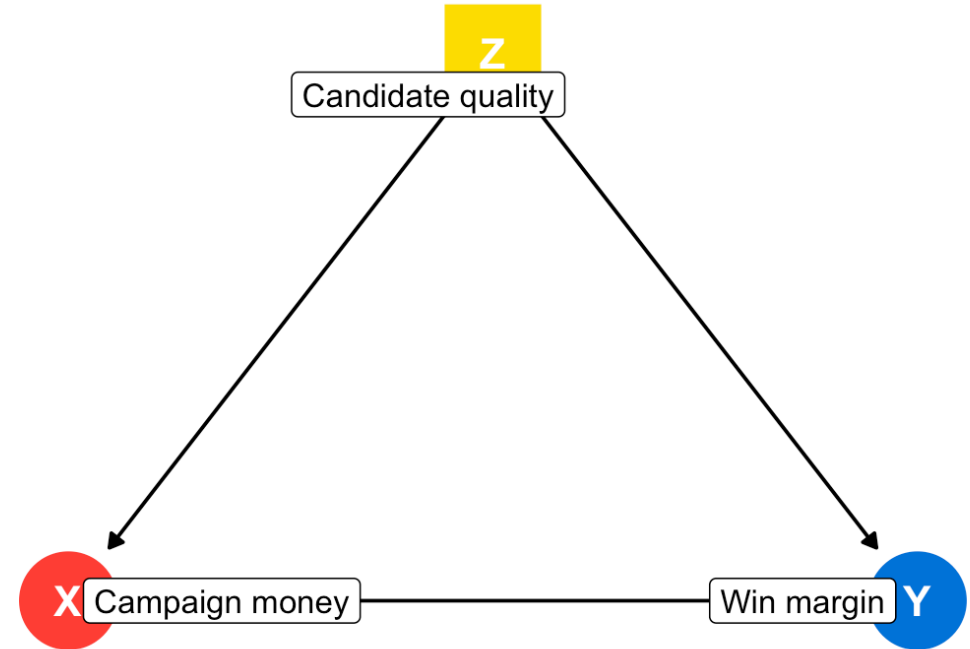


Closing doors

Find the part of campaign money that is explained by quality, remove it. This is the residual part of money.

Find the part of win margin that is explained by quality, remove it. This is the residual part of win margin.

Find the relationship between the residual part of money and residual part of win margin.
This is the causal effect.

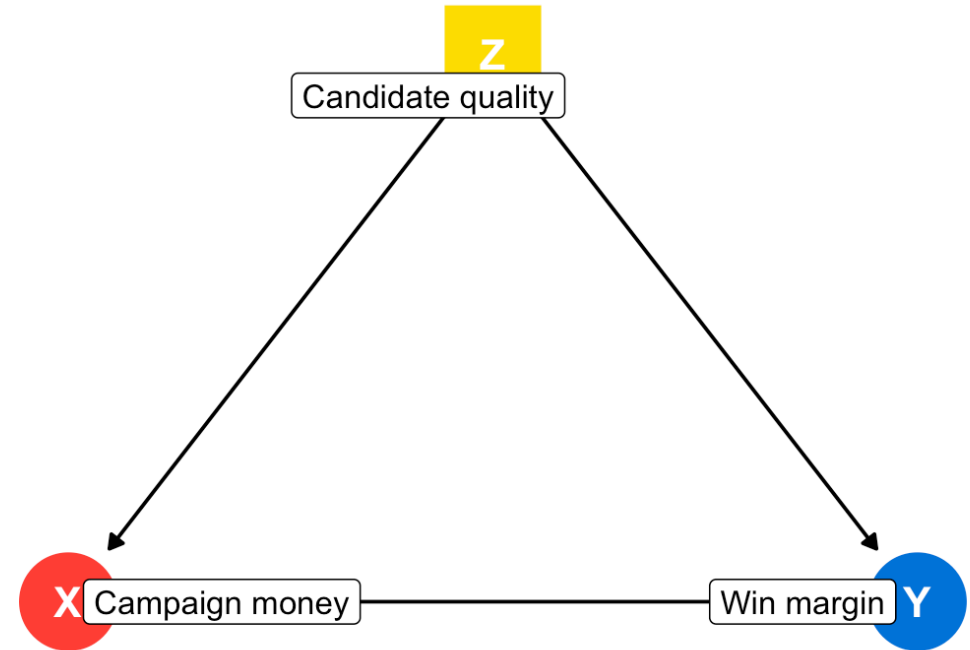


Closing doors

Compare candidates as if they had the same quality

Remove differences that are predicted by quality

Hold quality constant



How to adjust

Include term in regression

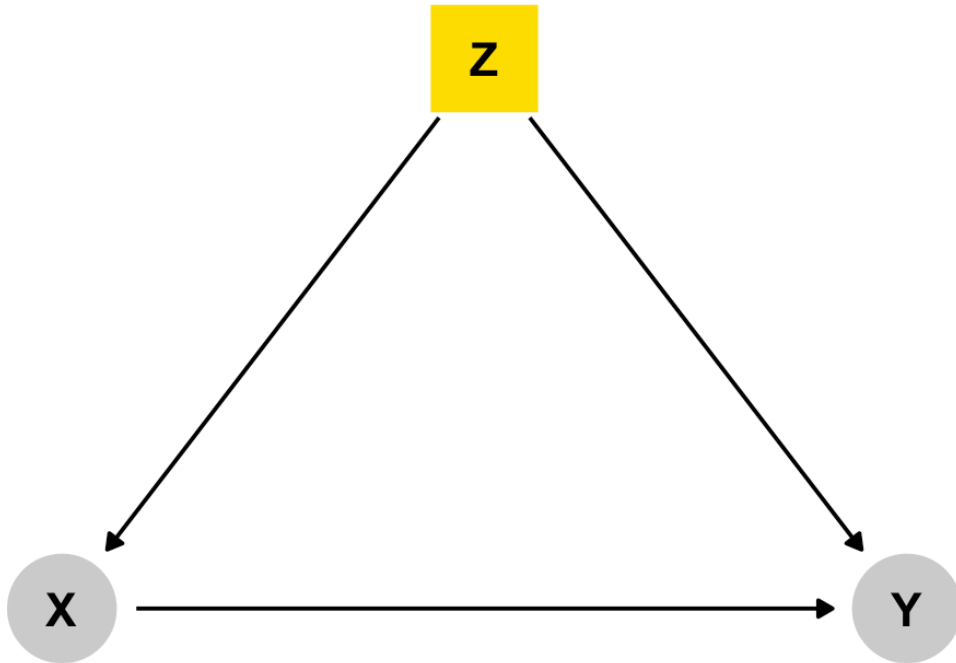
$$\text{Win margin} = \beta_0 + \beta_1 \text{Campaign money} + \beta_2 \text{Candidate quality} + \varepsilon$$

Matching

Stratifying

Inverse probability weighting

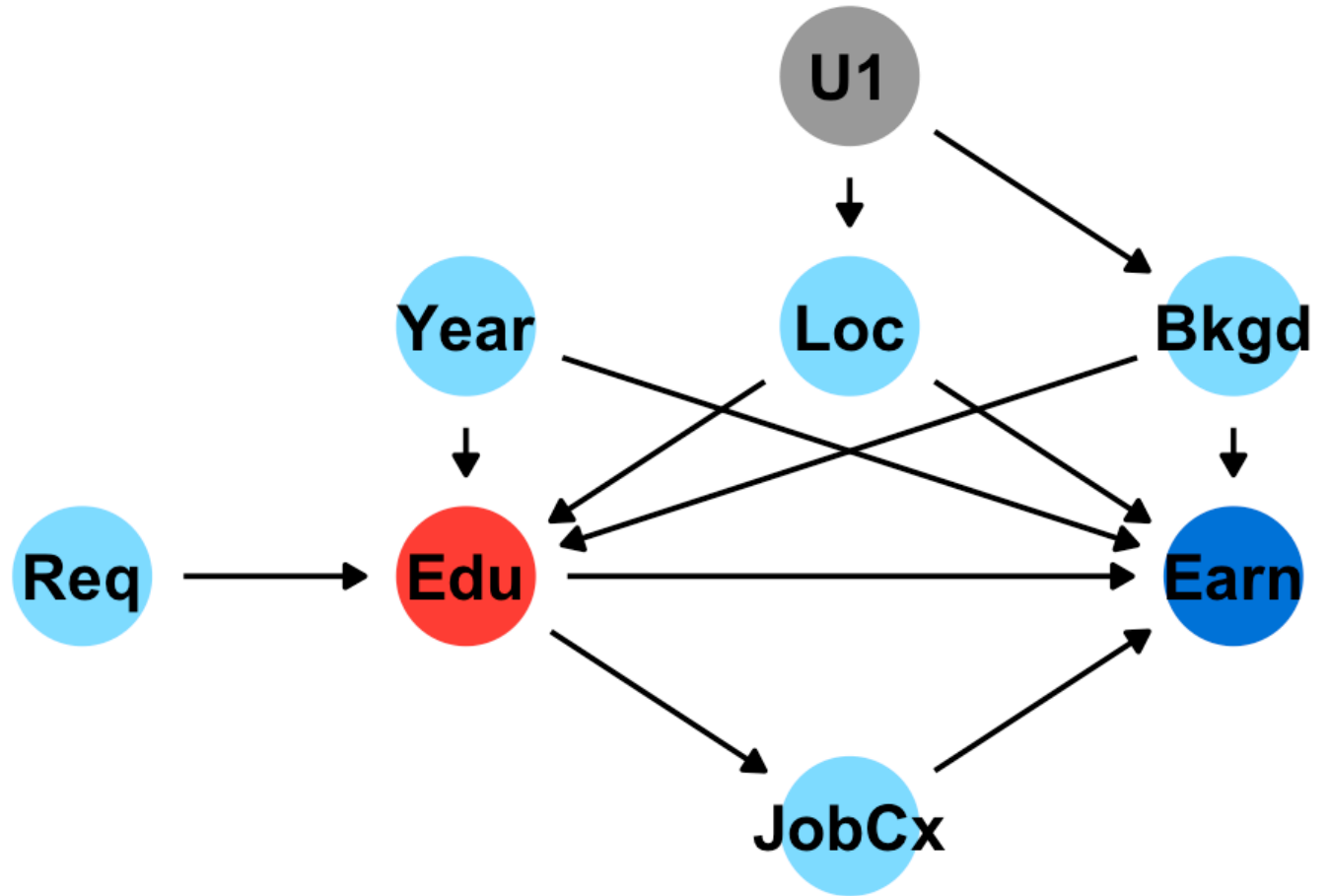
d-separation



If we control for **Z**,
X and **Y** are now
"*d*-separated" and
the association is
isolated!

Closing backdoors

Block all backdoor paths to identify the main pathway you care about



All paths

Education → Earnings

Education → Job connections → Earnings

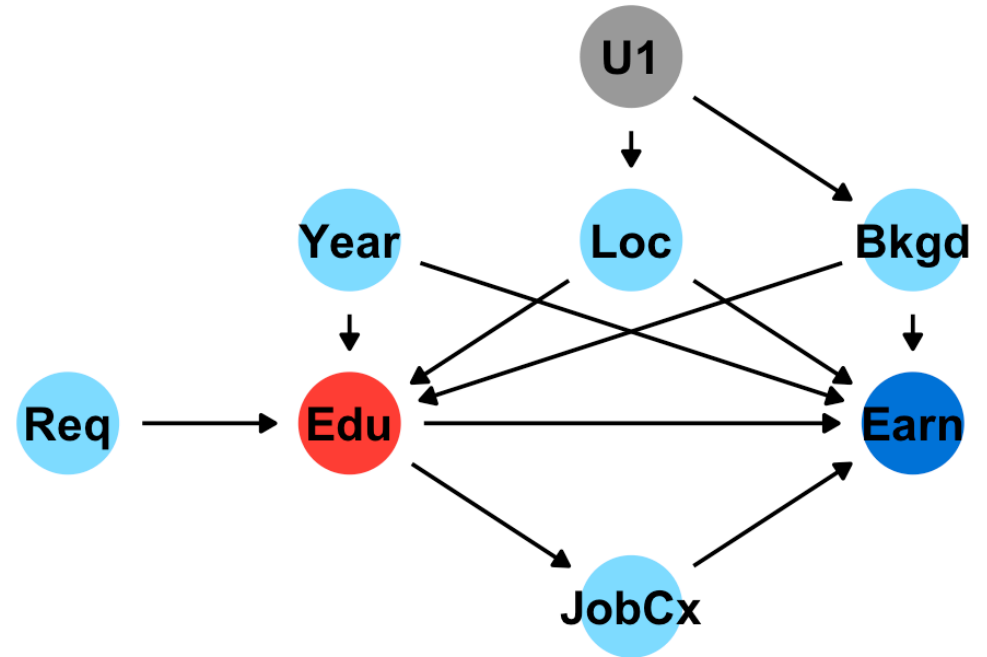
Education ← Background → Earnings

Education ← Background ← U1 → Location → Earnings

Education ← Location → Earnings

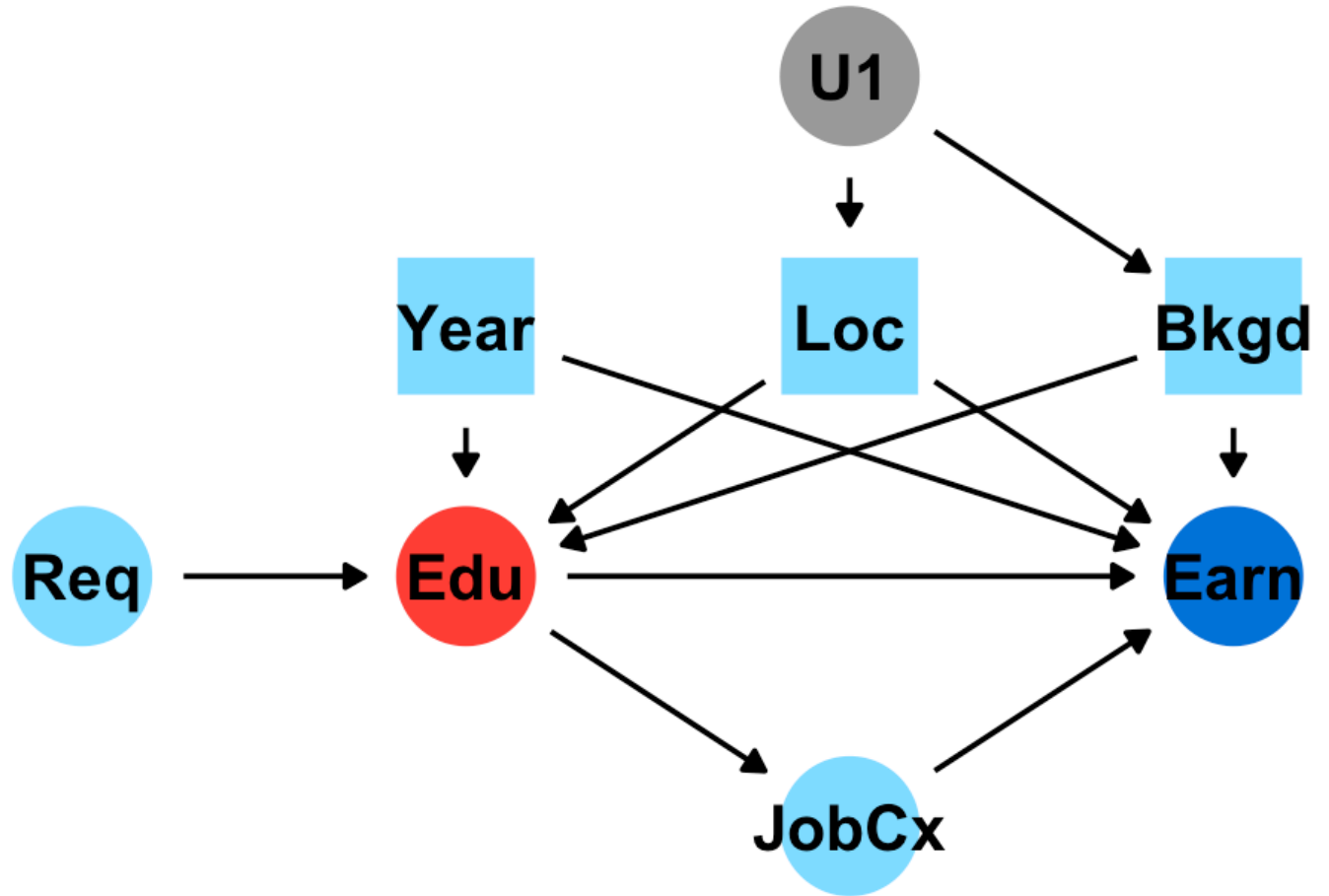
Education ← Location ← U1 → Background → Earnings

Education ← Year → Earnings



All paths

Adjust for **Location**,
Background and
Year to isolate the
Education →
Earnings causal
effect



Let the computer do this!

dagitty.net

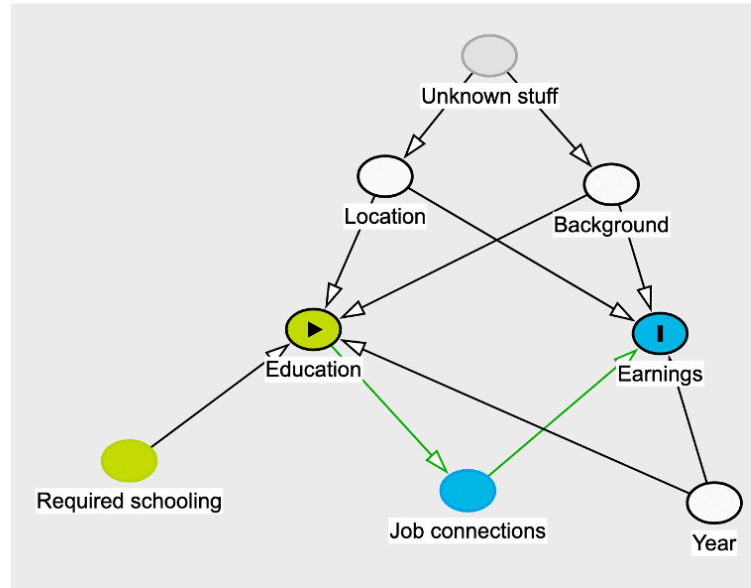
**The ggdag and dagitty
packages in R**

How do you know if this is right?

You can test the implications of the model to see if they're right in your data

$$X \perp Y \mid Z$$

X is independent of Y,
given Z

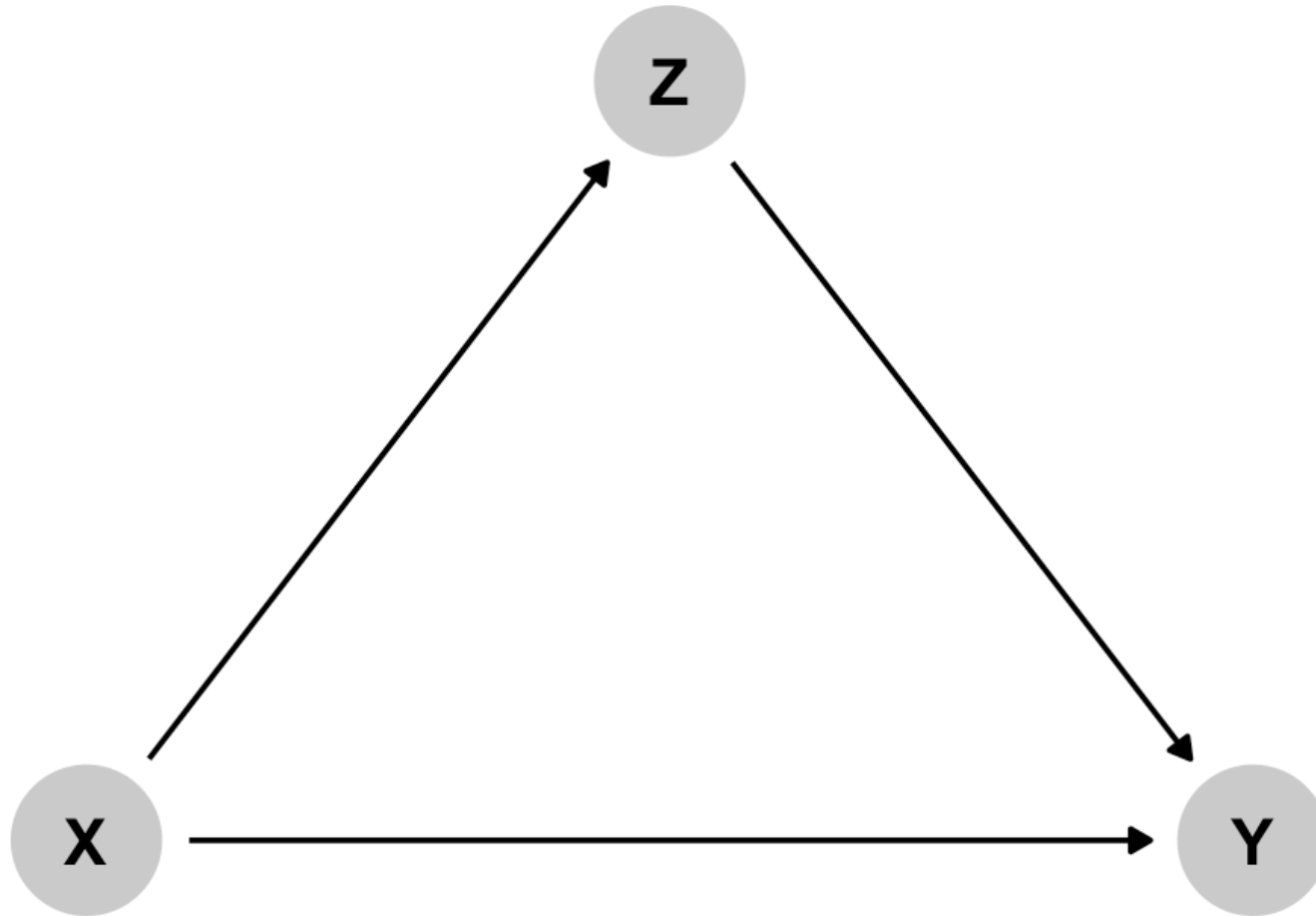


Testable implications

The model implies the following conditional independences:

- Education $\perp$ Earnings | Background, Job connections, Location, Year
- Required schooling $\perp$ Job connections | Education
- Required schooling $\perp$ Year
- Required schooling $\perp$ Earnings | Background, Job connections, Location, Year
- Required schooling $\perp$ Earnings | Background, Education, Location, Year
- Required schooling $\perp$ Background
- Required schooling $\perp$ Location
- Job connections $\perp$ Year | Education
- Job connections $\perp$ Background | Education
- Job connections $\perp$ Location | Education
- Year $\perp$ Background
- Year $\perp$ Location

Causation

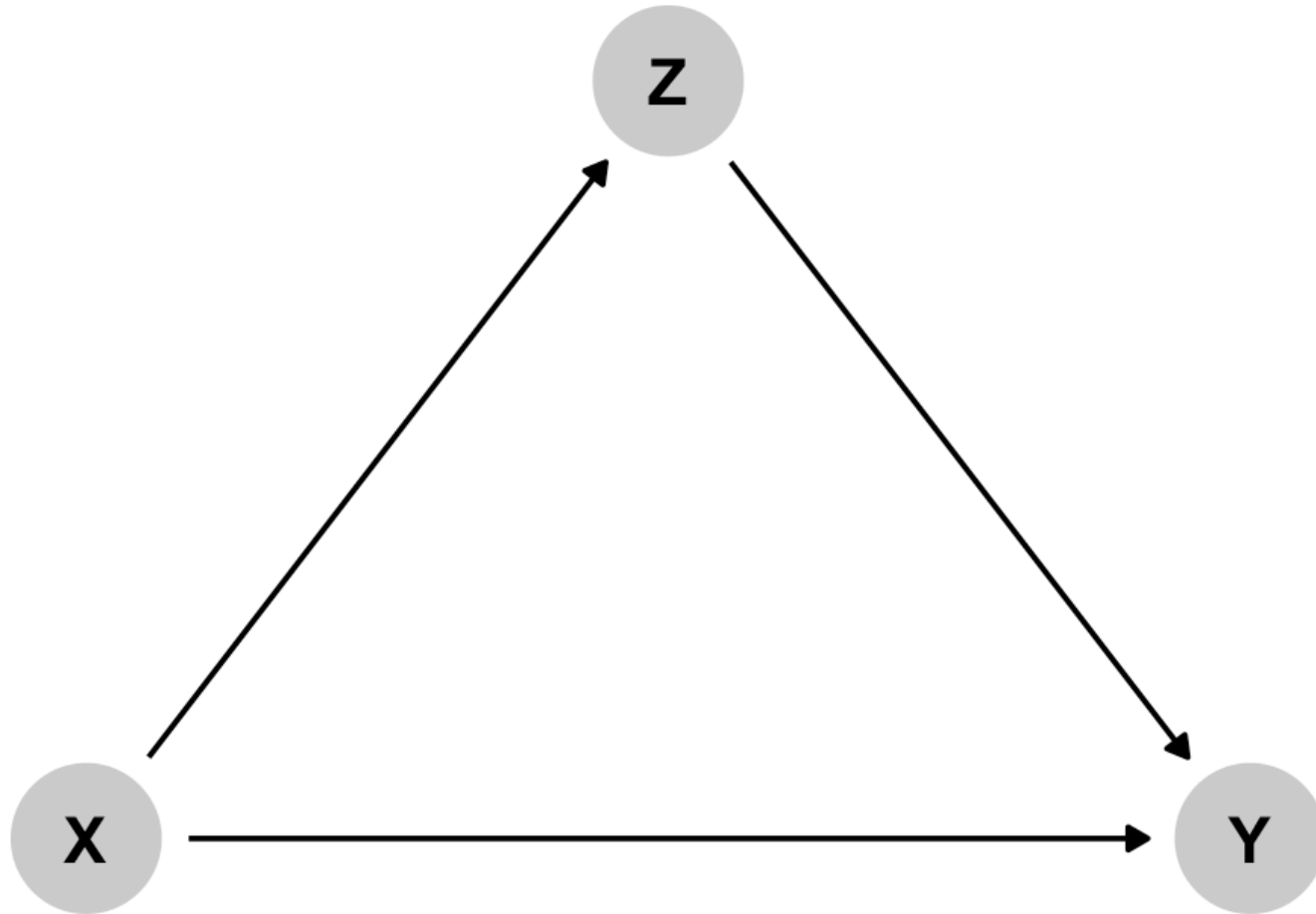


X causes Y

**X causes
Z which
causes Y**

**Should you
control for Z?**

Causation

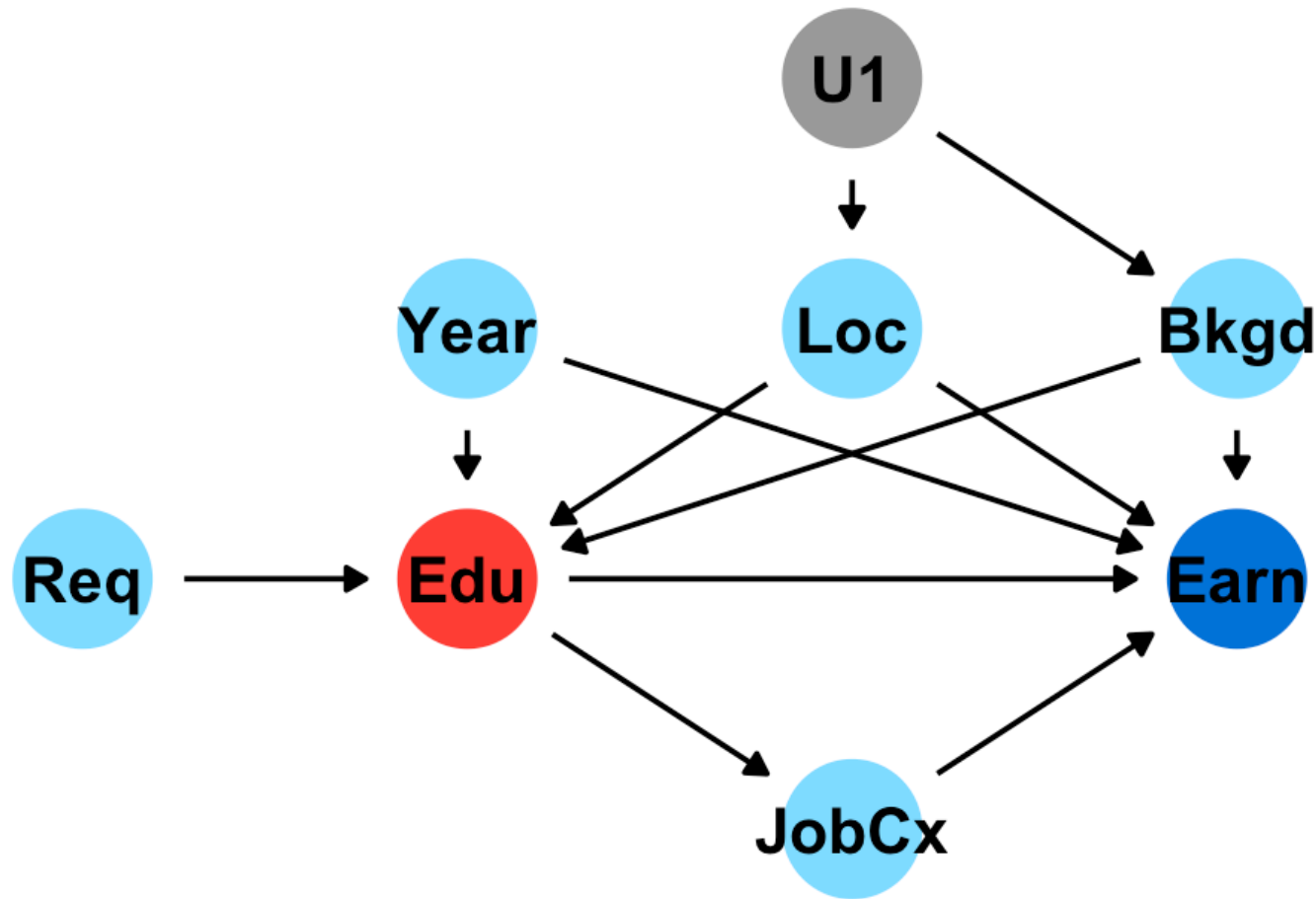


**Should you
control for Z?**

No!

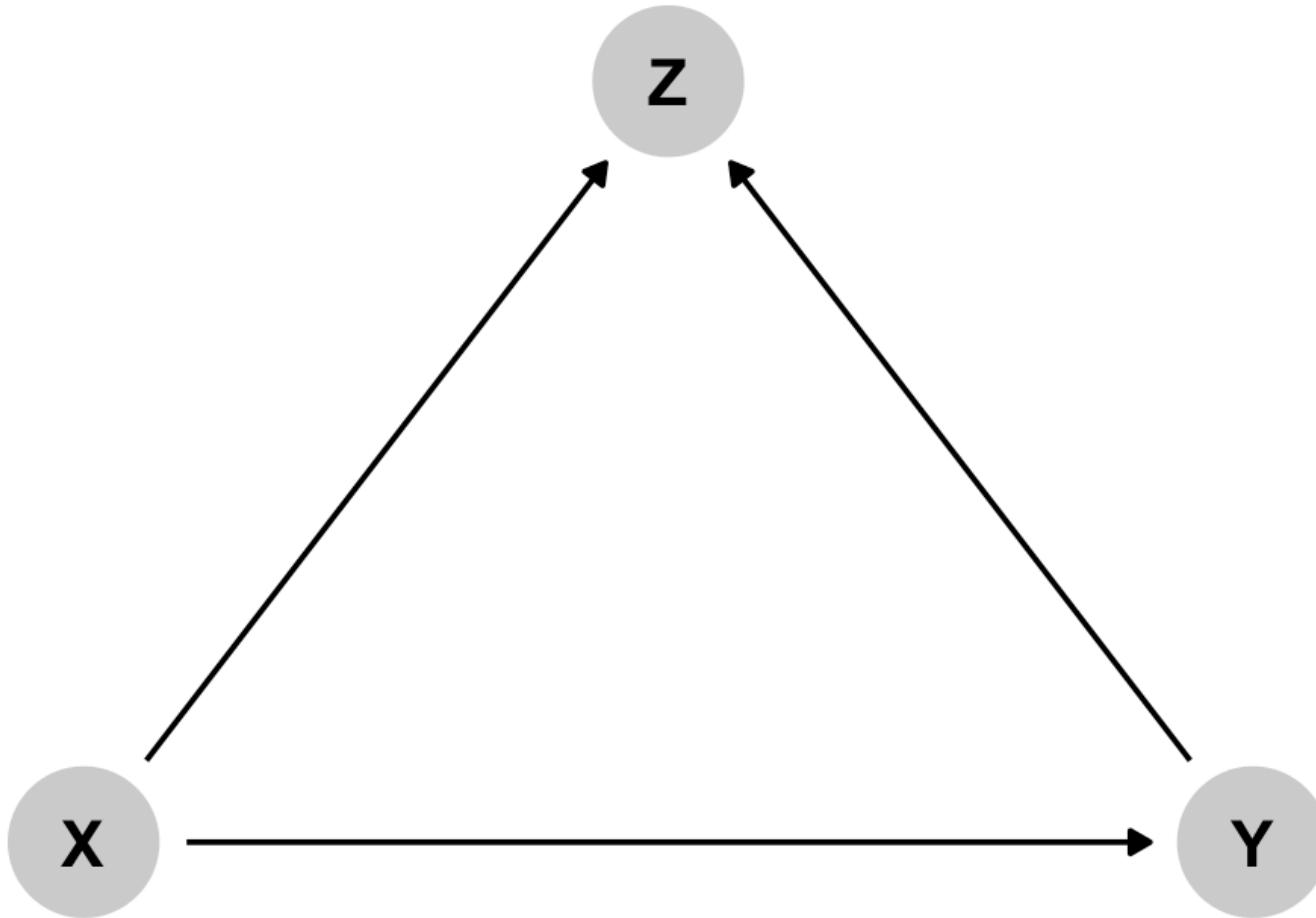
Overcontrolling

Causation and overcontrolling



Should you control
for job
connections?

Colliders



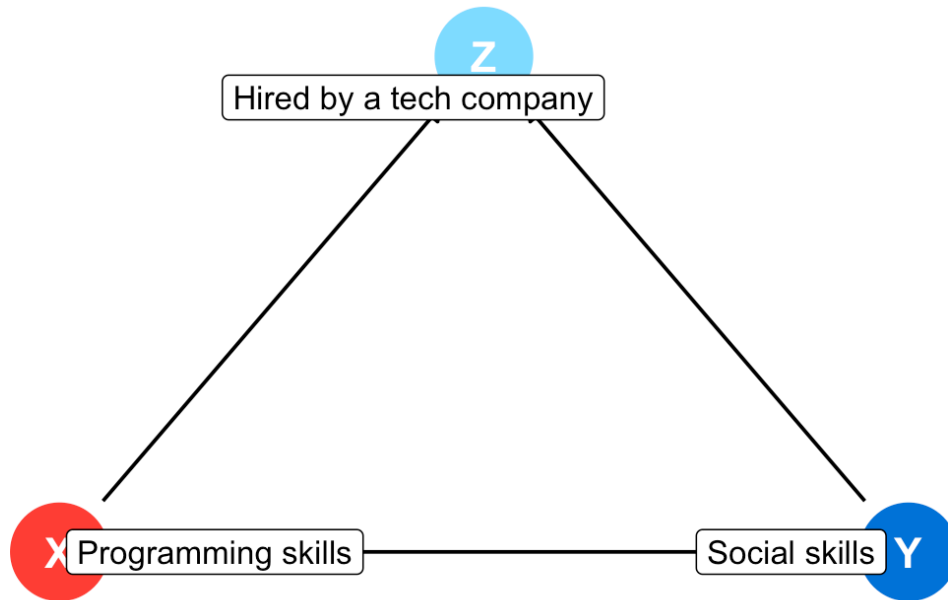
X causes Z

Y causes Z

**Should you
control for Z?**

Programming and social skills

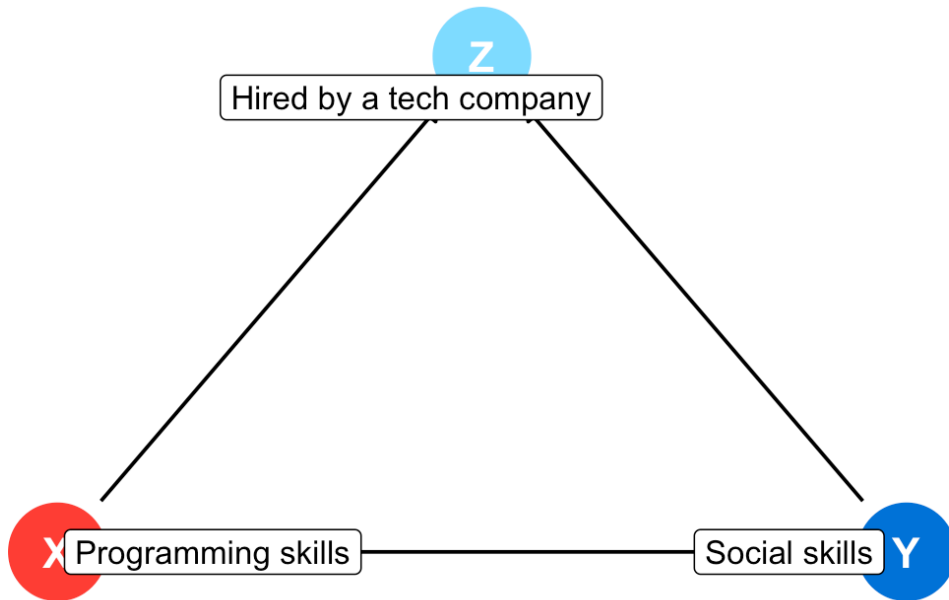
Do programming skills reduce social skills?



You go to a tech company and conduct a survey. You find a negative relationship!
Is it real?

Programming and social skills

Do programming skills reduce social skills?

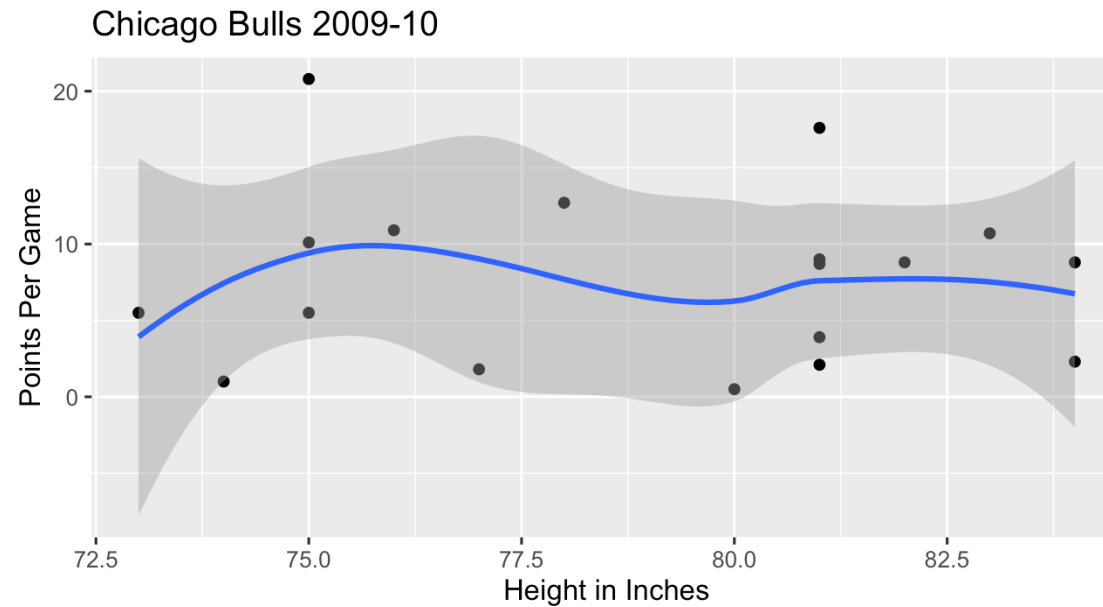


No! Hired by a tech company is a collider and we controlled for it.

This inadvertently connected the two.

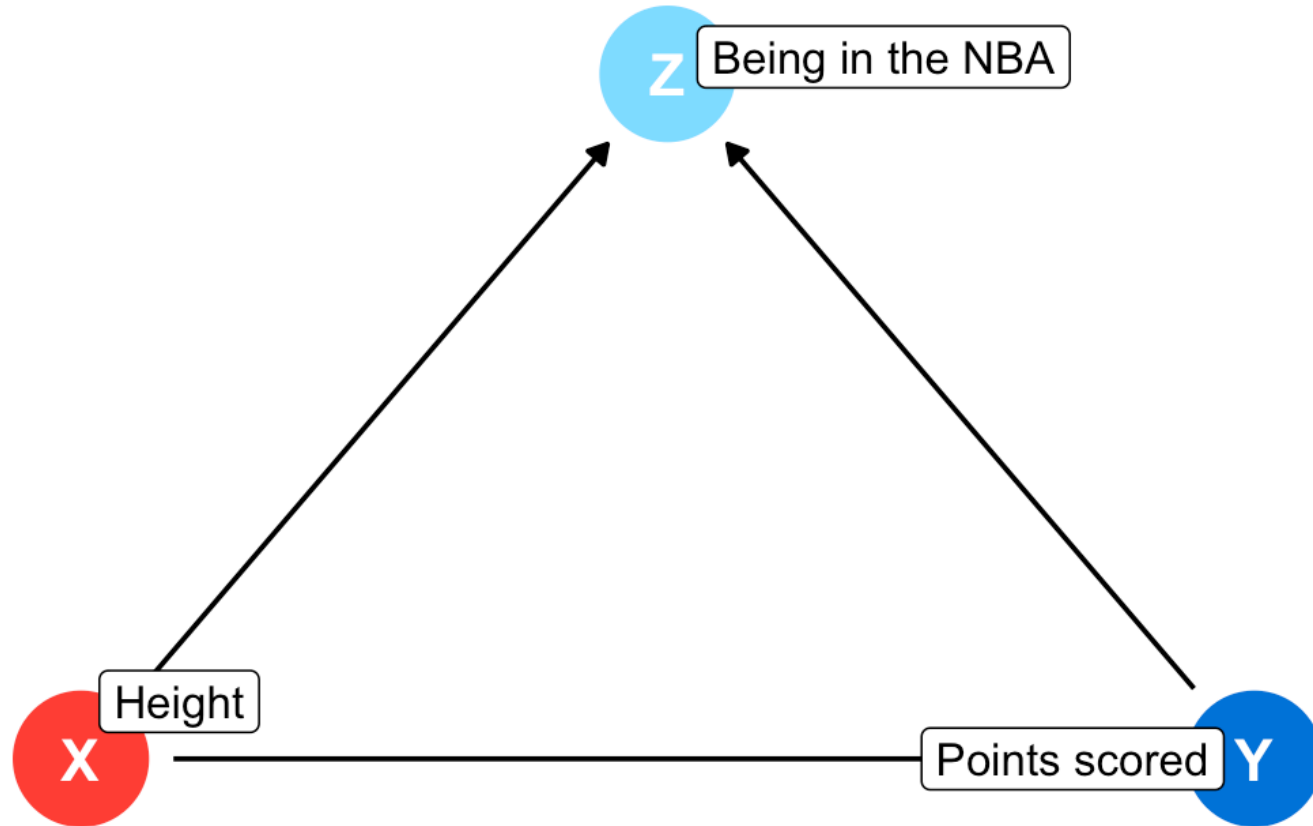
**Colliders can create
fake causal effects**

**Colliders can hide
real causal effects**



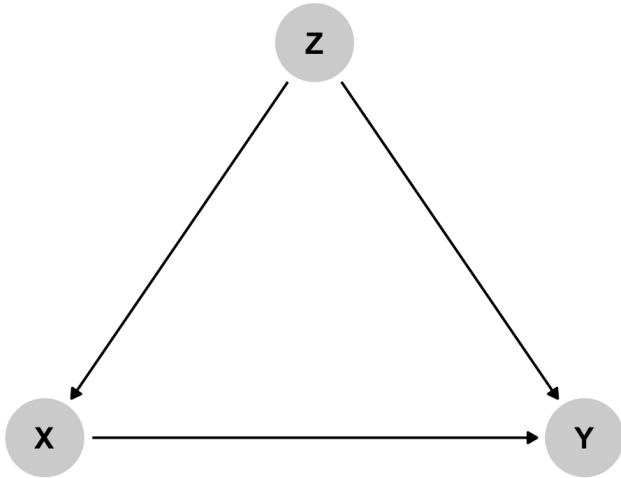
Height is unrelated to basketball skill... among NBA players

Colliders and selection bias



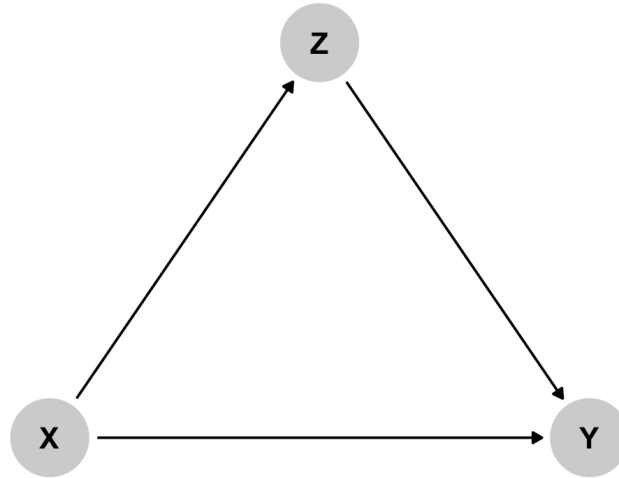
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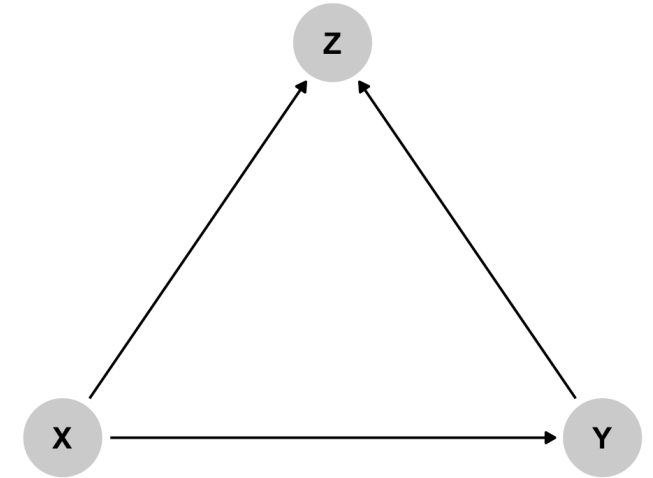
Common cause

Causation



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Selection /
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